

# MODELING OF PATTERN FORMATION DURING BRINE CHANNEL FORMATION

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## Macro-scale



$$\varphi(\eta) = \bigcup_{\alpha}^{\kappa} (\varphi(\eta))^{\alpha} = \bigcup_{\alpha}^{\kappa} \left( \bigcup_{\beta(\sigma)}^{\nu} (\varphi(\eta))^{\alpha\beta(\sigma)} \right)$$

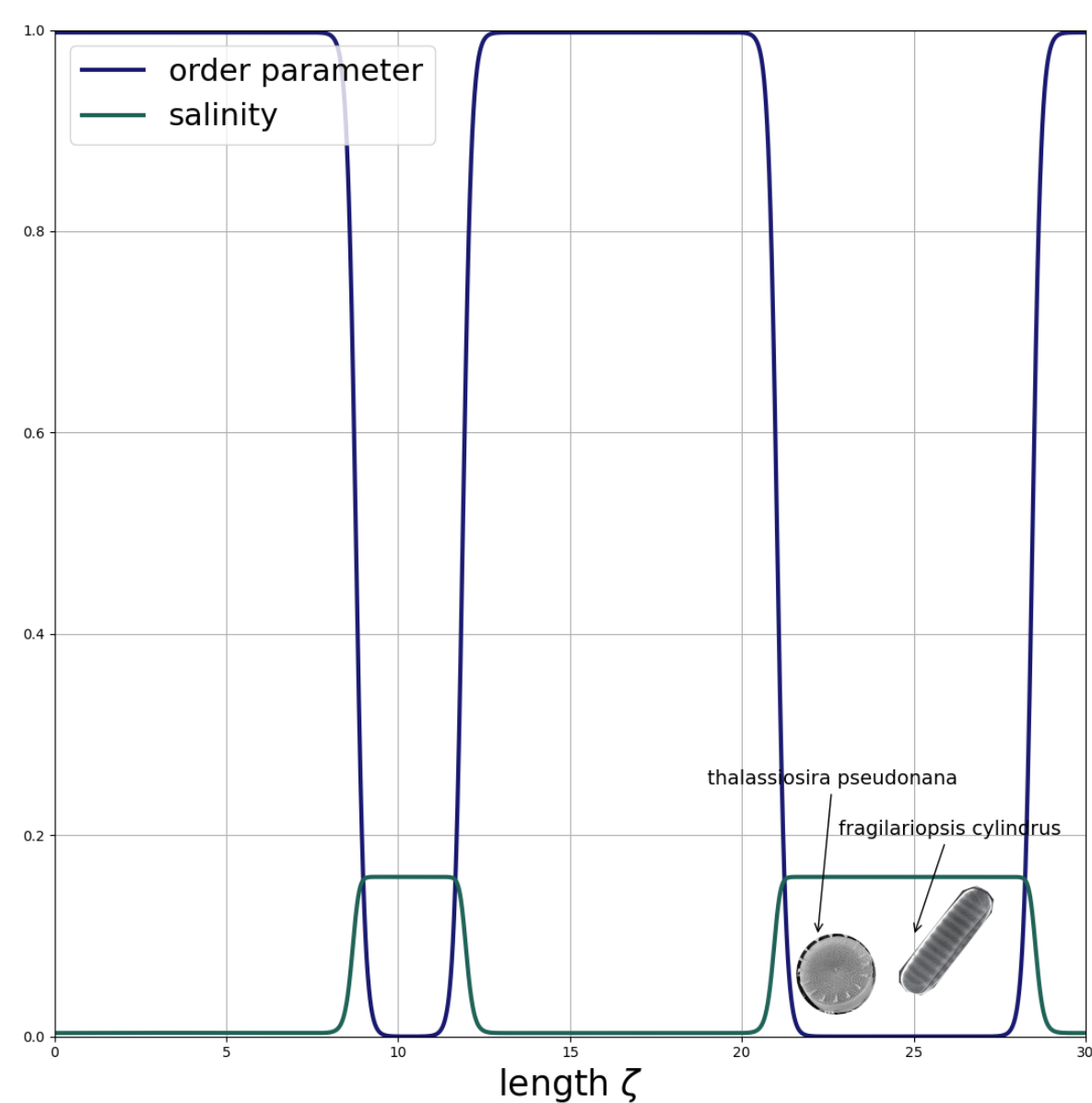
R. Pathak et al.<sup>1</sup>



**Coupling between macroscopic and microscopic order parameter  $\varphi \leftarrow \eta$  and macroscopic and microscopic salinity  $\beta \leftarrow \sigma$**



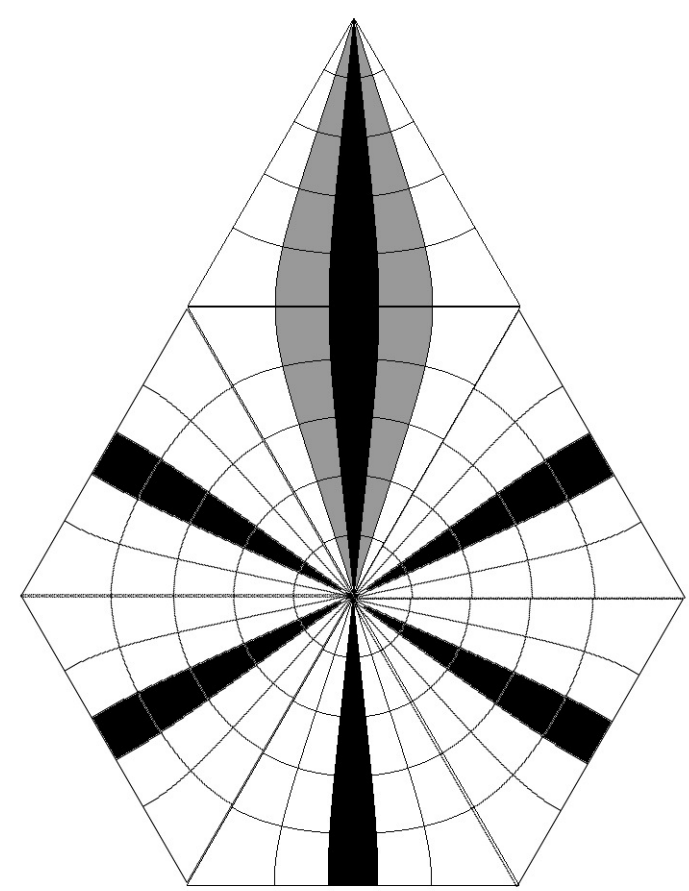
## Micro-scale



$$\begin{aligned} \tau_0 \frac{\partial \eta}{\partial \tau} &= -a^4 \eta \left( \eta - \frac{1}{4a} (3 - \sqrt{1 + 16m - 8\sigma}) \right) \left( \eta - \frac{1}{4a} (3 + \sqrt{1 + 16m - 8\sigma}) \right) + \frac{\partial}{\partial \zeta} \varepsilon^2 \frac{\partial}{\partial \zeta} \eta \\ \tau_0 \frac{\partial \sigma}{\partial \tau} &= \frac{\partial}{\partial \zeta} \varepsilon^2 \frac{\partial}{\partial \zeta} \left( \frac{1}{4} a^2 \eta^2 + \gamma \sigma \right) \end{aligned}$$

Scaled version of Thoms et al.<sup>2</sup> resp. Morawetz et al.<sup>3</sup>

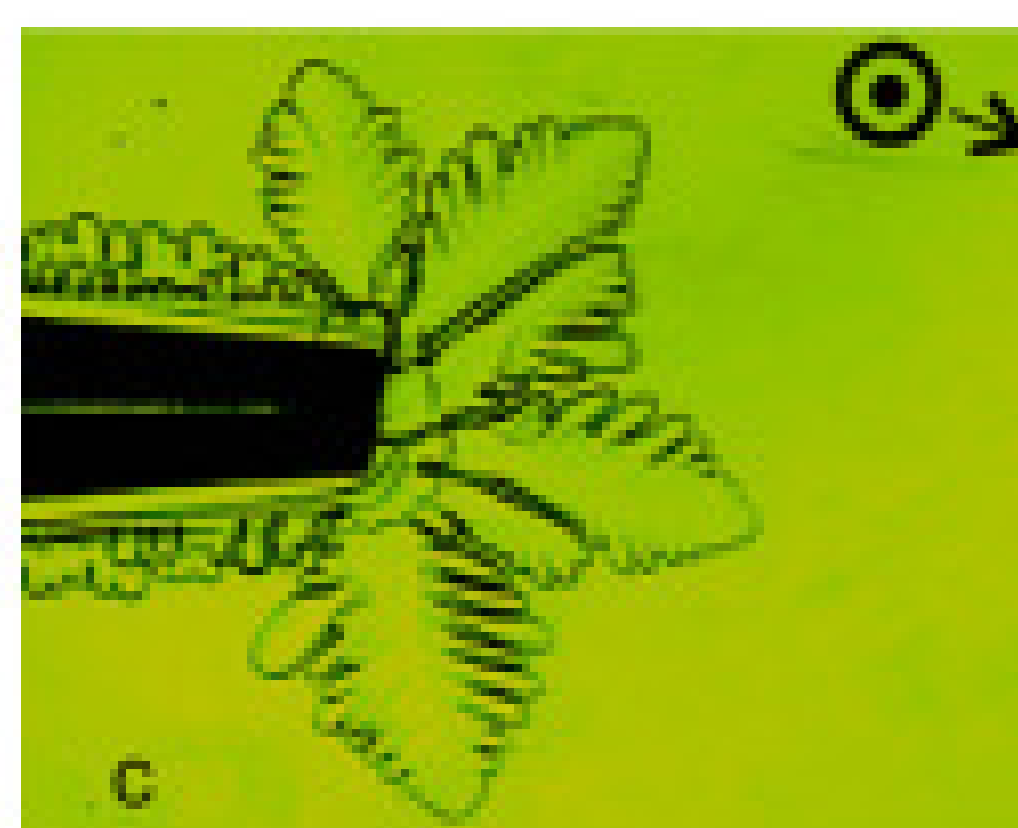
## Anisotropic enhancement



Schwarz-Christoffel transformation



Phase field simulation



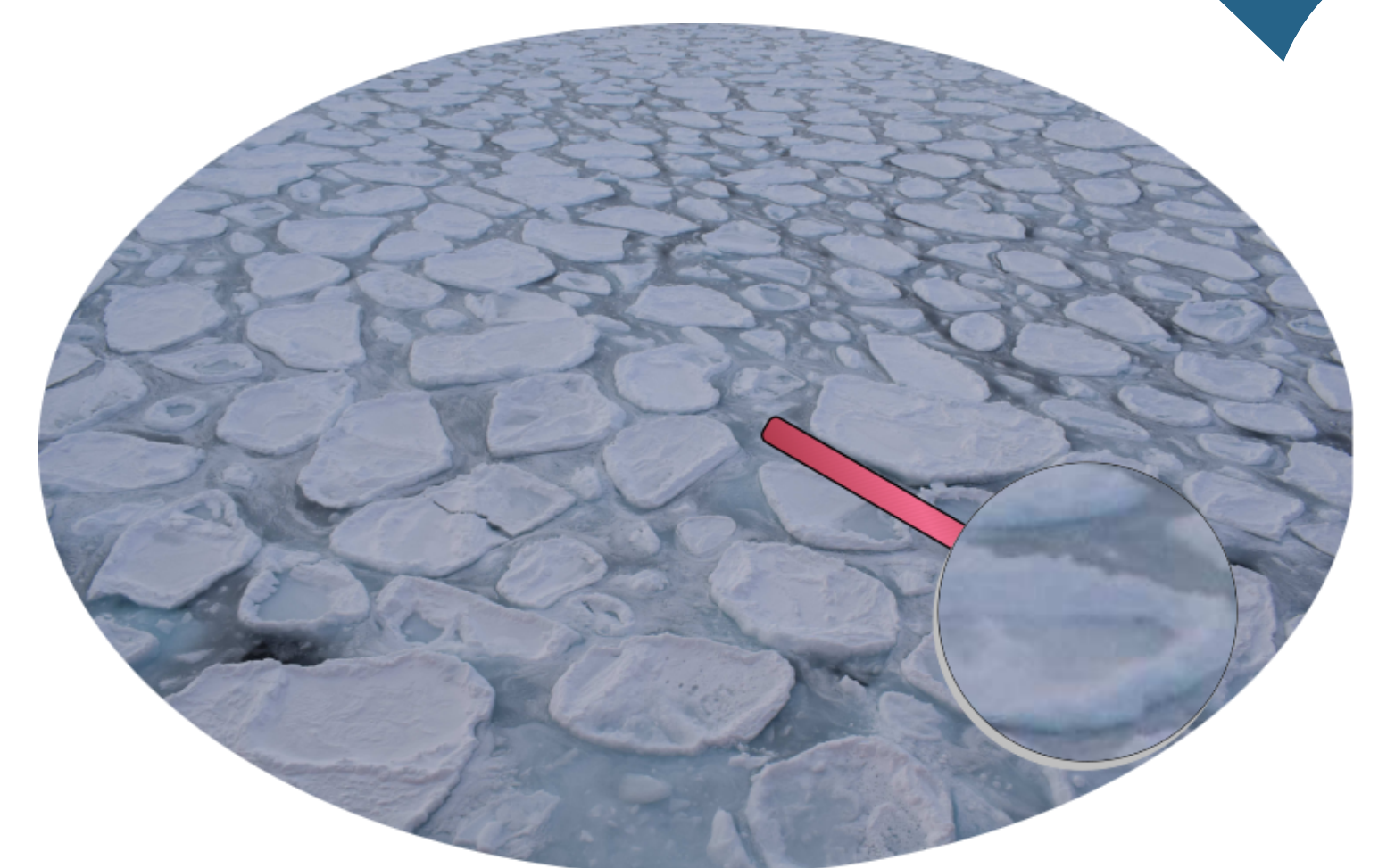
Different morphologies of ice single crystals observed by bright-field microscopy without AFPs (left) and with right  $\mu\text{M}$  (right)<sup>4</sup>



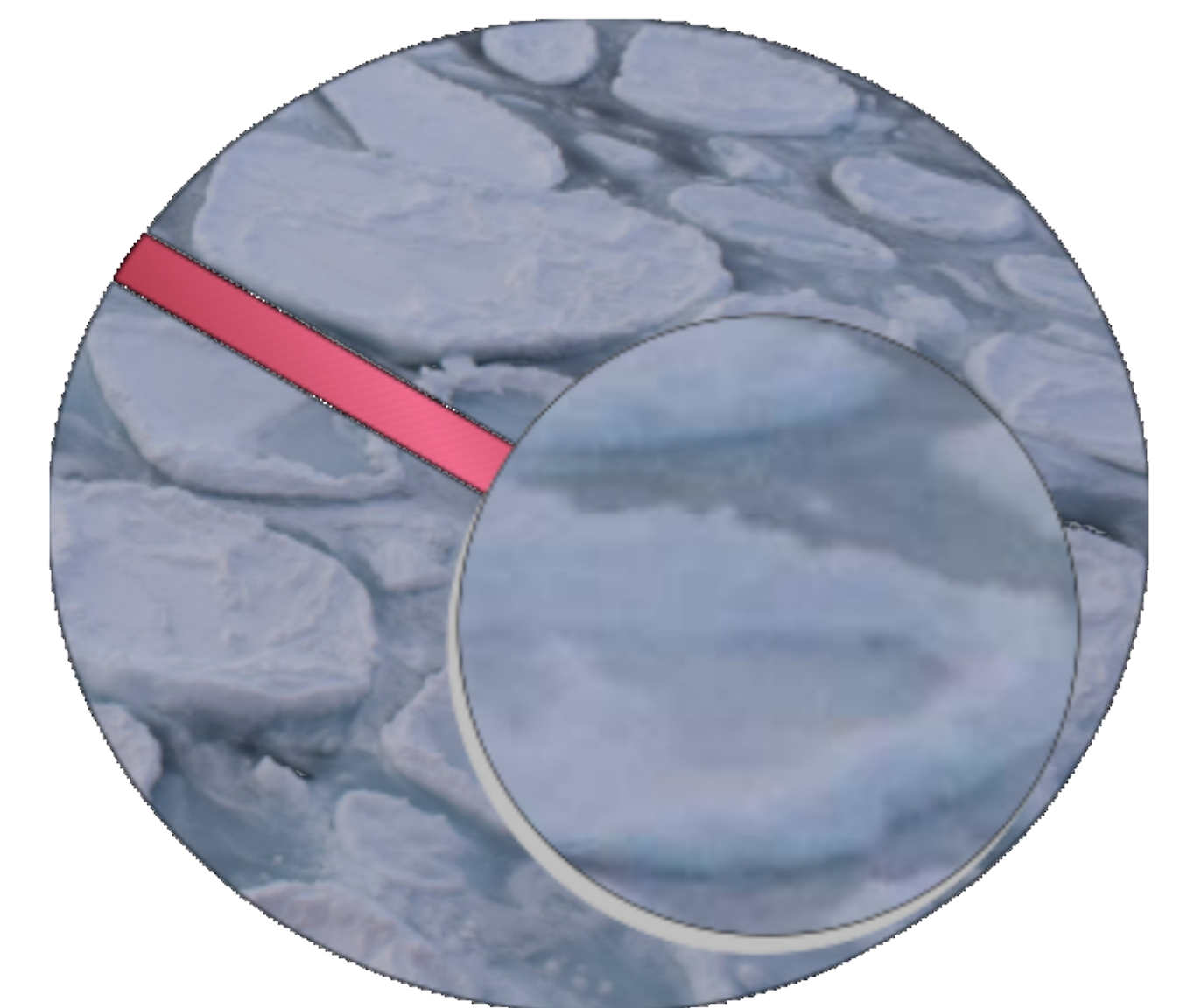
## References

1. Raghav Pathak, Seyed Morteza Seyedpour, Bernd Kutschan, Andrea Thom, Silke Thoms, Tim Ricken, "Modeling freezing and BioGeoChemical processes in Antarctic sea ice", Proc. Appl. Math. Mech., e202400047 (2024), <https://doi.org/10.1002/pamm.202400047>.
2. S. Thoms, B. Kutschan, K. Morawetz, (2014). "Phase-field theory of brine entrapment in sea ice: Short-time frozen microstructures". arXiv preprint arXiv:1405.0304.
3. K. Morawetz, S. Thoms, B. Kutschan, "Formation of brine channels in sea ice", Eur. Phys. J. E. 40: 25 (2017).
4. M. Bayer-Giraldi, Gen Sazaki, Ken Nagashima, Sepp Kipfstuhl, Dmitry A. Vorontsov, and Yoshinori Furukawa. "Growth suppression of ice crystal basal face in the presence of a moderate ice-binding protein does not confer hyperactivity", Proceedings of the National Academy of Sciences of the United States of America, 115(29) (2018). doi: <https://doi.org/10.1073/pnas.1807461115>.

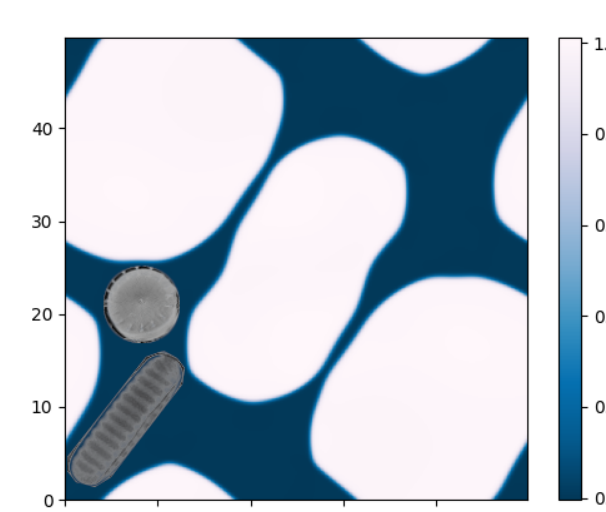
## Pancake ice



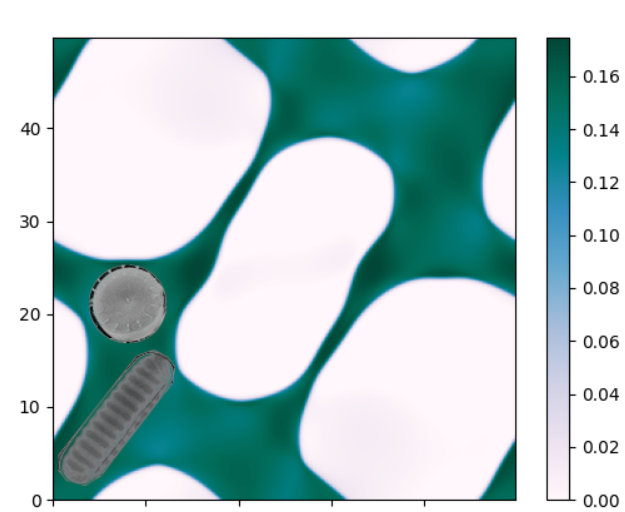
## Freezing process simulation



## Brine channels



Order parameter  $\eta$



Salinity  $\sigma$

## Nucleation process

