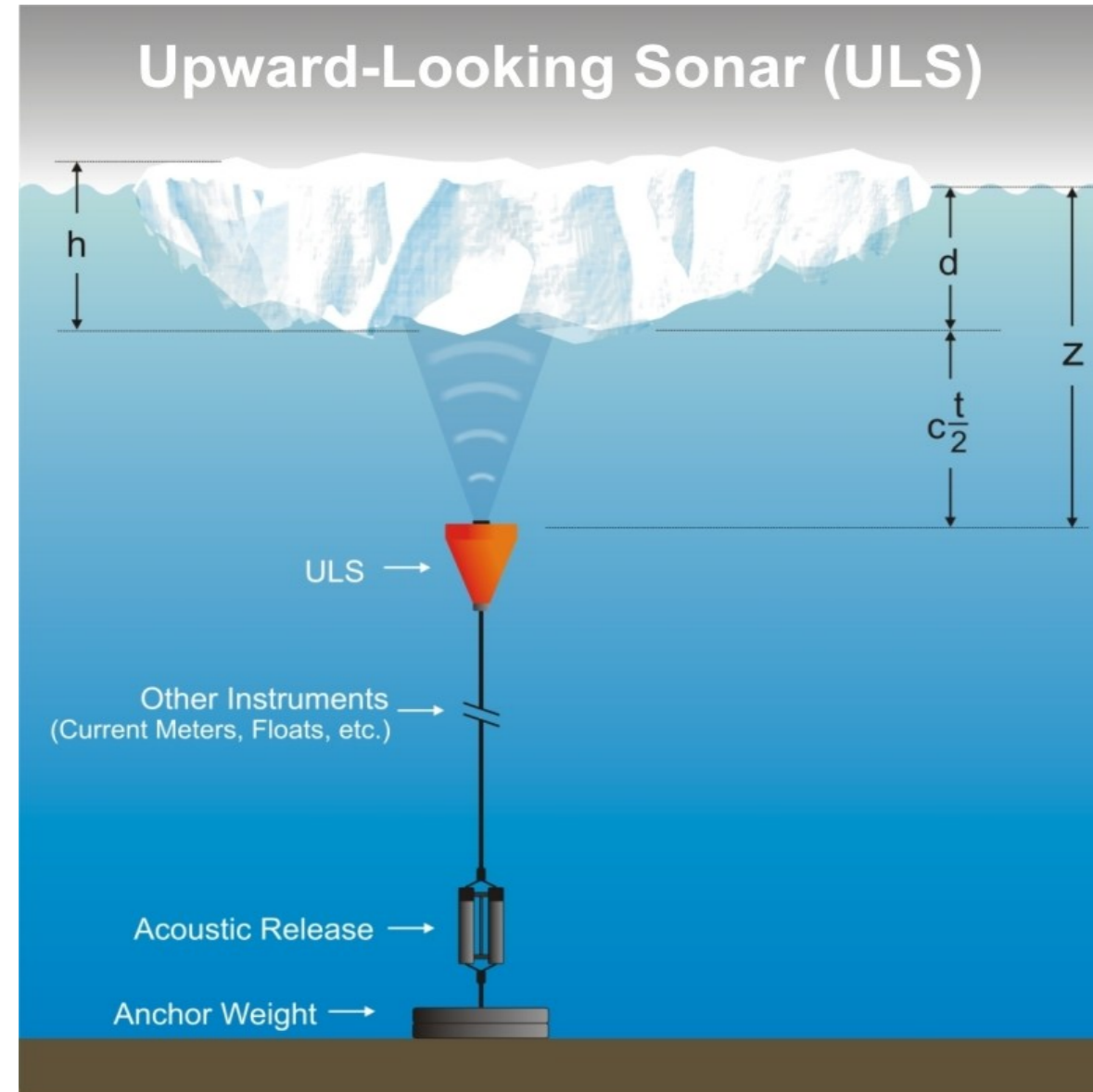


# Thermodynamic Growth of Sea Ice in the Weddell Sea

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 UND MEERESFORSCHUNG

## 1 Introduction & Objectives



h: Ice Thickness c: Sound Speed  
 d: Ice Draft t: Signal Travel Time  
 z: ULS Depth

**Fig. 1: Mooring arrangement with upward-looking sonar (ULS) [1].**

Thickness measurements of Southern Ocean sea ice are very sparse and satellite altimetry still provides relatively uncertain estimates of ice thickness. The only tool for monitoring sea ice thickness over long periods of time with sufficient accuracy are moored upward looking sonars (ULS). The instruments measure the subsurface portion (draft) of the ice by recording the travel times of sonar signals (Fig. 1). We present ULS data from the central Weddell Sea, where the sea ice starts forming in April and disappears in January of the following year (length of growth period: ~180 days).

We use the data together with Stefan's Law to estimate the two quantities that limit the maximum thermodynamic ice growth in austral winter to about 1 m: (a) The snow cover on top of the ice and (b) the oceanic heat flux from below.

## 3 Stefan's Law

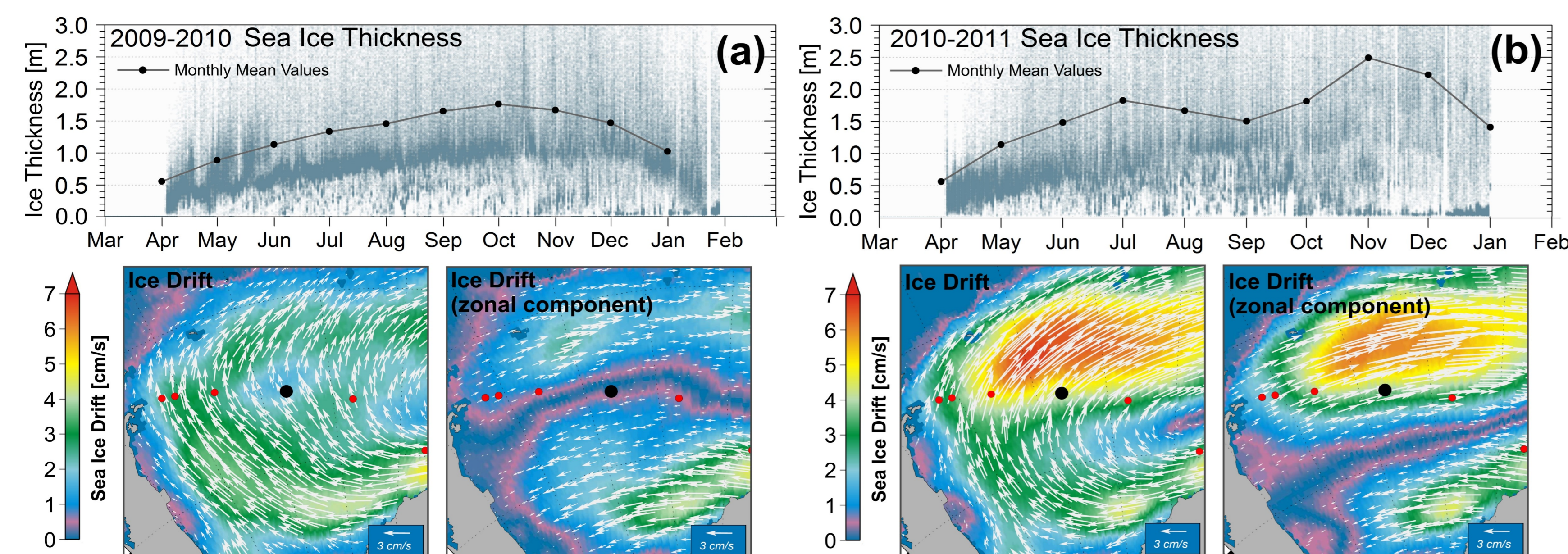
$$H = \sqrt{\frac{2\lambda_i}{\rho_i L_i \left(1 + \frac{\lambda_i}{\lambda_s r}\right)} \int_0^T (T_w - T_a) dt + A^2 - A - \frac{1}{\rho_i L_i} \int_0^T F_w dt}$$

$$A = \left( \frac{\lambda_i}{k \left(1 + \frac{\lambda_i}{\lambda_s r}\right)} \right) \text{ and } r = h/H$$

H: Ice Thickness  $T_{a,w}$ : Air/Water Temperature  
 h: Snow Layer Thickness k: Heat Transfer Coefficient  
 $\rho_i$ : Ice Density  $\lambda_{i,s}$ : Ice/Snow Thermal Conductivity  
 $L_i$ : Latent Heat of Ice  $F_w$ : Oceanic Heat Flux

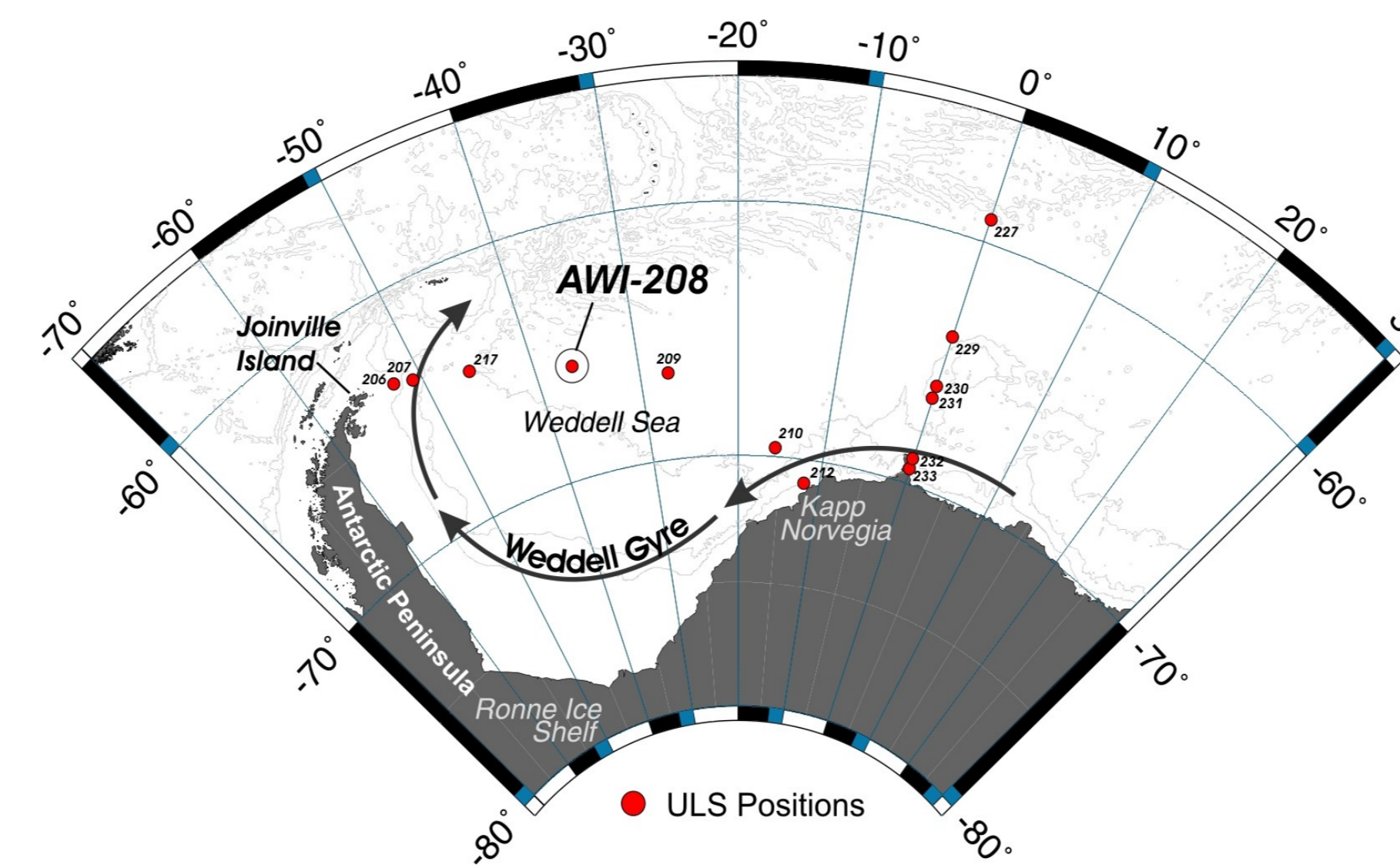
Modified form of Stefan's Law with ice-atmosphere coupling (k), a snow layer which is assumed to increase linearly with ice thickness ( $h = rH$ ) and a constant oceanic heat flux ( $F_w$ ) [2].

$\rho_i = 0.92 \text{ g cm}^{-3}$   $L_i = 334 \text{ J g}^{-1}$   
 $\lambda_i = 2.2 \text{ W m}^{-1} \text{ K}^{-1}$   $k = 22 \text{ W m}^{-2} \text{ K}^{-1}$   
 $\lambda_s = 0.19 \text{ W m}^{-1} \text{ K}^{-1}$



**Fig. 3: Upper panels: ULS draft data converted into total ice thickness. Each blue dot represents one ULS measurement (>500,000 per year). Lower panels: Average ice drift from microwave satellite sensors [3]. Black dot on drift maps: AWI-208. The drift was averaged for April-December. (a) Ice season 2009-2010. (b) Ice season 2010-2011.**

## 2 Data



**Fig. 2: Positions of the AWI mooring array in the Weddell Sea.**

The data for this study are from the ULS attached to mooring AWI-208 in the centre of the Weddell Gyre (Fig. 2). The ULS of AWI-208 measured in 1993-1994 with a lograte of 4 minutes and for three years between 2008-2010 with a lograte of 1 minute. The uncertainty of the ULS data was estimated as  $\pm 5$ -12 cm [1]. The surface air temperatures for calculating ice thickness using Stefan's Law were taken from the ECMWF Interim reanalysis project.

## 4 Results & Conclusion

Clear thermodynamic growth/melt cycles are measured at AWI-208 when the zonal ice drift component is small and/or has zero average (Fig. 3a). When the zonal ice drift dominates in eastern direction, the ULS measurements are more determined by deformed ice (Fig. 3b). To estimate the snow thickness and the oceanic heat flux, the ice draft from ULS was first converted into ice thickness. The thermodynamic growth was determined by calculating the statistical mode of the weekly ice thickness distributions. The observed ice growth can be reasonably described without assuming an oceanic heat flux (Fig. 4a). A slightly better fit, however, is obtained assuming a thinner snow cover and an additional moderate oceanic heat flux of  $7 \text{ W m}^{-2}$  (Fig. 4b).

Different combinations of  $r$  and  $F_w$  were calculated using Stefan's Law. Those results showing the smallest RMS deviation of 0.09 m from the ice-thickness mode were taken to derive realistic ranges of snow thickness and oceanic heat flux:  $0 \leq r \leq 0.06$  (i.e. ~0-6 cm snow) and  $5 \leq F_w \leq 12 \text{ W m}^{-2}$  (Fig. 4b). These values are within realistic boundaries for the Weddell Sea. For example, a heat flux of  $20 \text{ W m}^{-2}$  with  $r = 0.03$  would increase the RMS deviation to 0.47 m.

### Conclusions:

The modified form of Stefan's Law provides a reasonable model of thermodynamic ice growth in the Weddell Sea. Variations of the snow parameter and the oceanic heat flux within realistic boundaries suggest that both a snow layer of a few centimetres and a moderate oceanic heat flux limit the thermodynamic ice growth to about 1 m thickness in winter.

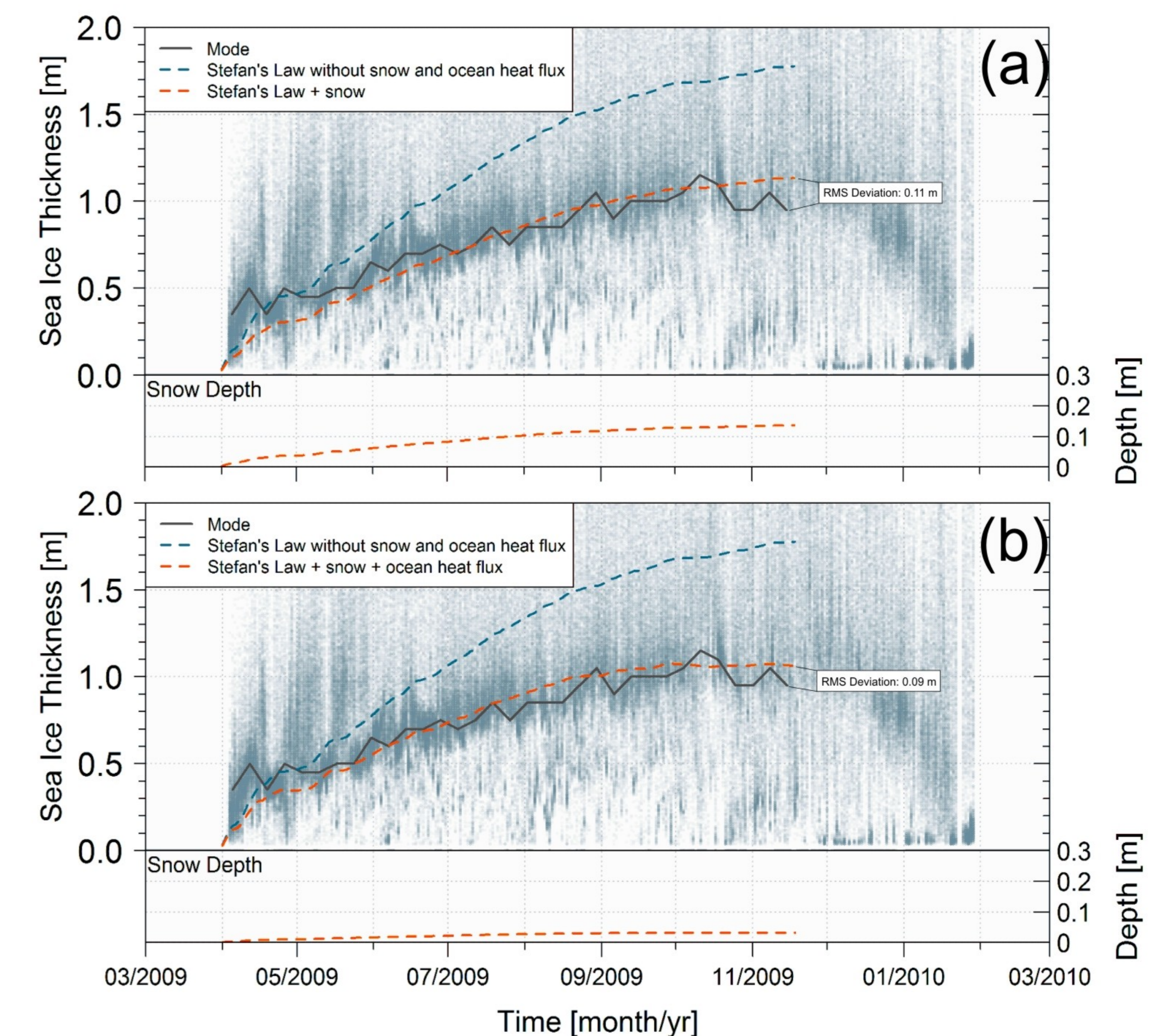
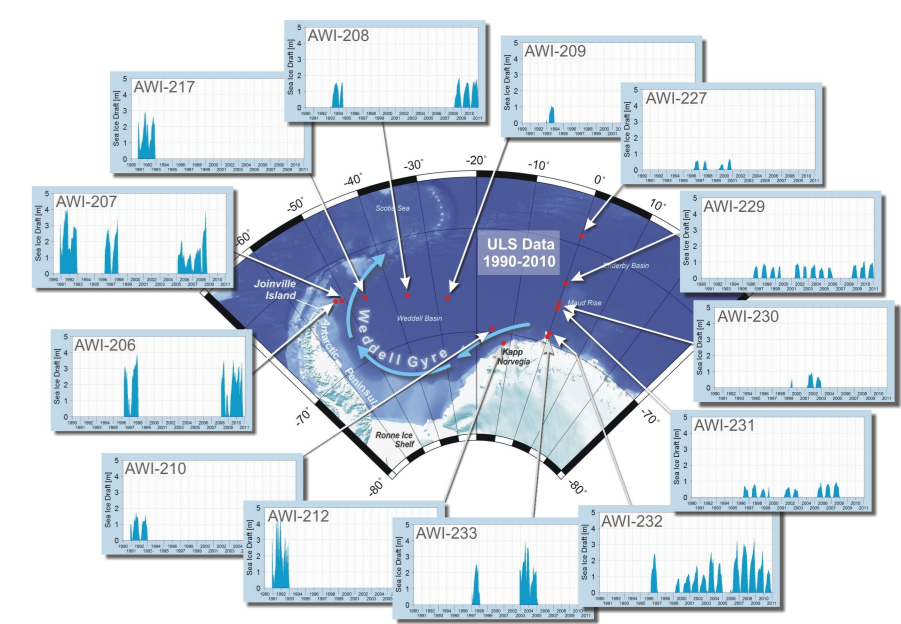
## References

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- [2] Petrich C., H. Eicken (2010) *Growth, Structure and Properties of Sea Ice*, In: Sea Ice (second edition), D.N. Thomas and G.S. Dieckmann (eds.), Blackwell Publishing Ltd.
- [3] Fowler C. (2013) *Polar Pathfinder Daily 25 km EASE-Grid Sea Ice Motion Vectors*, Boulder, Colorado USA: National Snow and Ice Data Center. Digital media.



Download the full ULS dataset from the PANGAEA archive:

doi: [10.1594 / PANGAEA . 785565](https://doi.org/10.1594/PANGAEA.785565)



**Fig. 4: ULS data for 2009-2010, the statistical mode of the weekly ice thickness distributions and estimations from Stefan's Law. Blue lines: results from Stefan's Law without snow and oceanic heat flux. (a) Red line: Model with snow layer and zero oceanic heat flux. (b) Red line: Model with thinner snow cover (~3 cm) and  $F_w = 7 \text{ W m}^{-2}$ . The subplots show the estimated snow layer thicknesses.**