Assimilating summer sea-ice thickness observations improves Arctic sea-ice forecast

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Key Points:

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12	٠	Assimilating summer CryoSat-2 sea-ice thickness (SIT) observations makes more
13		skillful Arctic ice-edge forecasts on multiple time scales.
14	•	The long-term SIT forecasts improve with the assimilation of summer CryoSat-
15		2 SIT observations.
16	•	Further refinement is needed for summer CryoSat-2 SIT observations.

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17 Abstract

Accurate Arctic sea-ice forecasting for the melt season is still a major challenge because of the 18 lack of reliable pan-Arctic summer sea-ice thickness (SIT) data. A new summer CryoSat-19 2 SIT observation dataset based on an artificial intelligence algorithm may alleviate this 20 situation. We assess the impact of this new dataset on the initialization of sea-ice forecasts 21 in the melt seasons of 2015 and 2016 in a coupled sea ice-ocean model with data assimilation. 22 We find that the assimilation of the summer CryoSat-2 SIT observations can reduce the 23 summer ice-edge forecast error. Further, adding SIT observations to an established forecast 24 system with sea-ice concentration assimilation leads to more realistic short-term summer 25 ice-edge forecasts in the Arctic Pacific sector. The long-term Arctic-wide SIT prediction 26 is also improved. In spite of remaining uncertainties, summer CrvoSat-2 SIT observations 27 have the potential to improve Arctic sea-ice forecast on multiple time scales. 28

²⁹ Plain Language Summary

Arctic sea ice is rapidly declining due to global warming, especially in summer. Accu-30 rate sea-ice forecasting is important to understand the potential influence of these changes 31 and devise effective responses. The performance of sea-ice forecasts highly depends on the 32 accuracy of the initial sea-ice states. So refining the initial conditions of sea-ice forecasts 33 with satellite observations is a common way to reduce forecast errors. However, obtain-34 ing reliable summer pan-Arctic satellite sea-ice thickness (SIT) data is challenging due to 35 complex ice-surface conditions in summer. A new artificial-intelligence-based summer SIT 36 satellite data product may improve initial SIT states. We integrate this dataset into a sea-ice 37 forecast system to evaluate its impact on forecast skill. We find that the new summer satel-38 lite SIT data can reduce short-term ice-edge location forecast errors and benefit long-term 39 SIT forecasts. 40

41 **1** Introduction

Arctic sea ice is declining at unprecedented speed (Rothrock et al., 1999; Comiso et al.,
2008; Kwok & Rothrock, 2009; Stroeve et al., 2012), which would pose challenges to climatic
and ecological stakeholders (Landrum & Holland, 2020). The Arctic Passage, opening up
with the gradually melting summer sea ice, calls for accurate Arctic sea-ice prediction from
daily to seasonal scales for safe navigation (Jung et al., 2016).

Accurate initialization of sea-ice state is vital for predicting Arctic sea ice (e.g., BlanchardWrigglesworth et al., 2011; Guemas et al., 2016; Xie et al., 2016; Dirkson et al., 2017; Bushuk
et al., 2022). The assimilation of sea-ice concentration (SIC) has improved the short-term
sea-ice forecasts greatly as documented in the literature, and is now widely used at forecasting centers (e.g., Hebert et al., 2015; Lemieux et al., 2015). Sea-ice thickness (SIT) persists
longer, therefore assimilation of SIT raises long-term sea-ice forecast skills even higher (Day,
Hawkins, & Tietsche, 2014; Shu et al., 2021; Mu et al., 2022).

However, the potential impacts of summer SIT observations on sea-ice forecasts are 54 not examined comprehensively yet due to a lack of data. An effective retrieval method for 55 the remotely sensed SIT from May to September was desired (Laxon et al., 2013; Ricker et 56 al., 2014). The complex summer ice-surface conditions restrict the application of classical 57 algorithms designed for winter conditions. For instance, melt ponds which occupy a huge 58 fraction of the sea-ice surface in the melt seasons (Maykut et al., 1992) complicate the clas-59 sification algorithms (Lee et al., 2018; Tilling et al., 2019) and introduce large uncertainties 60 due to increased moisture in the snow (Drinkwater, 1991). On the other hand, in-situ Arctic 61 SIT observations are rather scarce and localized, which can be hardly used for assimilation 62 due to their limited spatial representation within a relatively large model grid cell. 63

In a recent study, Dawson et al. (2022) presented the first estimate of pan-Arctic summer 64 sea-ice freeboard from radar altimeter by using a 1D convolutional neural network (CNN) 65 to distinguish ice leads from melt ponds. Landy et al. (2022) converted summer CryoSat-2 66 radar freeboard to SIT and applied further corrections. The spring predictability barrier of 67 the Arctic sea ice (e.g., Day, Tietsche, & Hawkins, 2014; Bushuk et al., 2017) suggests that 68 sea-ice forecast should benefit from the initialization with SIT in the melt season (Bushuk et 69 al., 2020). Therefore, it presents an opportunity to explore the extent to which the summer 70 SIT observation could improve the real-time forecast skill. Min et al. (2023) demonstrated 71 that assimilation of summer SIT corrects the overestimation in the Combined Model and 72 Satellite Thickness (CMST; Mu et al., 2018b) product. Y.-F. Zhang et al. (2023) found 73 that the assimilation of May to August CryoSat-2 SIT anomalies improves local SIC and 74 sea-ice extent (SIE) forecasts in September. However, the influence of assimilating summer 75 CryoSat-2 SIT observations on short-term sea-ice forecast in summer and on long-term 76 forecast extending beyond September still needs further investigation. 77

In this study, we focus on the impact of summer SIT observations on the daily and seasonal forecast skills of a sea-ice prediction modelling system. In particular, we perform a series of short- and long-term ensemble sea-ice forecasts where the sea ice-ocean initial state is constrained by the summer CryoSat-2 SIT or where these data are not used. The benefits and challenges of using these new SIT data are evaluated and critically discussed using independent sea-ice data.

⁸⁴ 2 Data and Methods

2.1 The coupled sea ice-ocean model

We use a regional coupled sea ice-ocean model driven by atmospheric forecasts to con-86 figure the sea ice-ocean forecast system. The model is based on the Massachusetts Institute 87 of Technology general circulation model (MITgcm; Marshall et al., 1997) and covers the 88 pan-Arctic region with a horizontal resolution of around 18 km as in Losch et al. (2010). 89 The sea-ice model uses a viscous-plastic rheology (Hibler III, 1979; J. Zhang & Hibler III, 90 1997) and a zero-layer thermodynamic formulation without heat capacity (Semtner, 1976; 91 Parkinson & Washington, 1979). The readers are referred to Losch et al. (2010) and Nguyen 92 et al. (2011) for more details on the model. 93

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2.2 Data assimilation and forecast

The summer data assimilation system is initialized from restart files generated by CMST 95 (Mu et al., 2018b) simulation with 11 ensemble members. CMST combines model physics 96 with information from remote-sensed SIT and SIC observations. It successfully reproduces 97 the spatio-temporal sea-ice variations (Mu et al., 2018b). In this study, the summer data 98 assimilation and forecast strategy follows Mu et al. (2019). All observations and corre-99 sponding uncertainties are interpolated onto the 18-km model grid for assimilation. After 100 the assimilation of sea-ice observations using a Local Error Subspace Transform Kalman 101 Filter (Nerger et al., 2012) coded within the Parallel Data Assimilation Framework (Nerger 102 et al., 2005), the ensemble sea-ice forecasts start from the new analyses and are integrated 103 forced by the atmospheric forecasts (cf. Section 2.3). More details on the data assimilation 104 and forecast system are given in Supporting Information. 105

The 80-km-resolution CryoSat-2 summer SIT data set is derived from local variations in the CryoSat-2 radar echo response using a deep learning method (Dawson et al., 2022; Landy et al., 2022). This is the first estimate of pan-Arctic summer SIT from satellite observations. The summer SIT is assimilated into the system on a daily basis using the observations linearly interpolated between two biweekly (twice per month) records. However, the roughness-induced electromagnetic range bias on the heavily-deformed ice in the coast regions leads to significant SIT underestimate north of the CAA and Greenland in late

summer (Landy et al., 2022). Practically we set the observation uncertainties higher than 113 the original values over thick ice regions, while still using the provided errors over thin ice 114 regions (Supporting Information). The SIC data used in the assimilation are computed at 115 the French Research Institute for Exploitation of the Sea (IFREMER) based on the 85-GHz 116 SSM/I and SSM/IS channels with a resolution of 12.5 km (Kaleschke et al., 2001; Spreen 117 et al., 2008: Kern et al., 2010). The uncertainty of the SIC observation is set to a constant 118 value of 0.25 following Yang, Losa, Losch, Jung, and Nerger (2015). 119

The short-term ensemble assimilation and forecast experiments are driven by the 174-120 121 hour atmospheric ensemble forecasts from the United Kingdom Met Office (UKMO) Ensemble Prediction System (EPS; Bowler et al., 2008). For the long-term prediction, the 122 ensemble members are driven by deterministic atmospheric forcing (single member). The 123 atmospheric forecasts from the NCEP Climate Forecast System Version 2 (CFSv2; Saha et 124 al., 2014) are used for the 9-month long-term forecasts, while the ECMWF Reanalysis v5 125 (ERA5; Hersbach et al., 2020) is used as the atmospheric forcing during the data assimila-126 tion to minimize the potential error caused by deviations of atmospheric forcing during this 127 period. 128

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2.3 Experiment design

In order to investigate the potential impact of the CryoSat-2 summer SIT on sea-ice 130 forecasts, this study designs both short-term (7 days) and long-term (270 days) forecasts 131 (Table. 1). These experiments are conducted over different months. The short-term experi-132 ments in 2015, which cover the melt season, start from the CMST restart files on May 1, May 133 31, June 30, July 30, and August 29, respectively. Each forecast experiment lasts for 30 days 134 and on each day a 7-day sea-ice forecast is run using the atmospheric forcing from the daily 135 UKMO ensemble forecasts. No data assimilation is applied in the control run of the short-136 term forecasts (Short-CTRL). The Short-SIT experiments assimilate only the CryoSat-2 137 summer SIT data, and the Short-SIC experiments assimilate only the SSMI/SSMIS SIC 138 data, while both data sets are assimilated in the Short-SICSIT experiments. For the 2016 139 experiments, only the start dates are changed to match the available restart files from CMST 140 (Table. 1). 141

The long-term forecast experiments are designed to diagnose the persistence of the 142 assimilated CryoSat-2 summer SIT over the months from the melt season to the freezing 143 season. The Long-SIT, Long-SIC and Long-SICSIT experiments with data assimilation 144 start each summer month from CMST restart files. Unlike the incremental analysis update 145 approach, the state vector is updated each day directly in the next 15 days to assimilate 146 observations. Over that period, ERA5 atmospheric reanalysis forcing is used. Then, the 147 270-day sea-ice forecasts start from the sea-ice analysis restart files and are forced by the 148 CFSv2 operational atmospheric forecasts. No data assimilation is performed in the Long-149 CTRL experiments. The forecast start dates are listed in Table 1. 150

2.4 Verification 151

Airborne electromagnetic SIT observations north of Greenland from AWI IceBird cam-152 paigns in July and August 2016 are employed for comparison with the assimilation results. 153 Locations of these observations are indicated in Figure S1. The integrated ice-edge error 154 (IIEE; Goessling et al., 2016) is used to quantify the skill of the short-term ice-edge fore-155 casts. It measures the discrepancy between the forecasted and observed SIE. The reference 156 observation used in this study is the 25-km-resolution NOAA/NSIDC Climate Data Record 157 (CDR) of Passive Microwave Sea Ice Concentration Version 4 (Meier et al., 2021). 158

To validate the skill of the long-term sea-ice forecast, we compute the IIEE and the 159 RMSD of SIT against various other products and in-situ observations. The IIEE is still com-160 puted using the NOAA/NSIDC CDR data. The RMSDs of SIT are computed with respect 161

Table 1. Summary of forecast experiments design. The number in the parenthesis representsthe size of atmospheric forcing ensemble. Short: short-term forecast. Long: long-term forecast.SIC: sea-ice concentration. SIT: sea-ice thickness.

Experiment	Assimilated data	Forecast duration (days)	Atmospheric forcing during assimilation	Atmospheric forcing during forecast	Forecast start date
Short-CTRL	/	7	UKMO (11)	UKMO (11)	Daily forecast starting from 01 May 2015,
Short-SIT	CryoSat-2 SIT	7	UKMO (11)	UKMO (11)	31 May 2015, 30 Jun 2015, 30 Jul 2015, 29 Aug 2015, 25 Apr 2016, 25 May 2016,
Short-SIC	SSMI/SSMIS SIC	7	UKMO (11)	UKMO (11)	
Short-SICSIT	SSMI/SSMIS SIC and CryoSat-2 SIT	7	UKMO (11)	UKMO (11)	24 Jun 2016, 24 Jul 2016, 23 Aug 2016.
Long-CTRL	/	270	ERA5 (1)	CFSv2(1)	16 May 2015, 15 Jun 2015,
Long-SIT	CryoSat-2 SIT	14	15 Jul 2015, 14 Aug 2015, 13 Sep 2015,		
Long-SIC	SSMI/SSMIS SIC	270	ERA5 (1)	CFSv2(1)	 10 May 2016, 09 Jun 2016, 09 Jul 2016, 08 Aug 2016, 07 Sep 2016.
Long-SICSIT	SSMI/SSMIS SIC and CryoSat-2 SIT	270	ERA5 (1)	CFSv2(1)	

to the 25-km-resolution CS2SMOS products (Ricker et al., 2017) when they are available be-162 tween October and the following April. Both NOAA/NSIDC CDR and CS2SMOS data are 163 interpolated onto the 18-km grid to calculate the IIEE and RMSD. Note that CS2SMOS is a 164 merged product using winter Cryosat-2 and Soil Moisture Ocean Salinity (SMOS) SIT. The 165 SIT observations derived from upward-looking sonar moorings maintained by the Beaufort 166 Gyre Exploration Program (BGEP) are used for the forecast evaluation. The three moorings 167 BGEP-A, BGEP-B, and BGEP-D, which provide year-round sea-ice draft observations, are 168 located at (75.0°N, 150.0°W), (78.0°N, 150.0°W) and (74.0°N, 140.0°W), respectively (Figure 169 S1). The draft is converted to SIT by multiplying it by a constant factor of 1.1 as in Nguyen 170 et al. (2011). 171

172 **3 Result**

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3.1 Short-term ice-edge forecast

SIT from CryoSat-2 and the short-term experiments in 2015 is shown in Figure 1. 174 The spatially averaged SIT differences between Short-SIT and Short-CTRL from May to 175 September 2015 are 0.10 m, -0.06 m, -0.37 m, -0.37 m and -0.39 m, respectively. Overall, 176 the SIT differences are smallest in May and June, when the assimilation of the summer 177 CryoSat-2 observations reduces the SIT in the Pacific sector and increases it in the Atlantic 178 sector (regions shown in Figure S1). Along with higher uncertainties in the CryoSat-2 SIT 179 observations due to strong ice melting in July, August and September, a remarkable SIT 180 reduction over the multi-year ice regions (regions shown in Figure S2) is found. SIT is also 181 reduced in most of the marginal ice zones, especially in the Beaufort Sea and the Chukchi 182 Sea. In our experiment, SIC assimilation, however, has only limited impact on SIT near 183 the ice edge due to reliable restart states from CMST system that already has assimilated 184 SIC observations. The absolute spatially averaged SIT differences between Short-SIC and 185 Short-CTRL are minor, within 0.04 m. In the sea ice interior region with SIC close to 1.0 186 far from the ice edge, SIC assimilation can hardly further improve the SIT there by means 187 of the covariance matrix, due to a narrow SIC ensemble spread. Similar results are also 188 found in 2016 (Figure S3). 189

Assimilating summer CryoSat-2 SIT in Short-SIT gives rise to a more reasonable SIT 190 probability density distribution along the trajectories of the IceBird campaigns north of 191 Greenland (Figure S4), particularly for the modal SIT. Overestimation in CMST as indi-192 cated by Short-CTRL is significantly reduced. The median SIT difference against IceBird 193 observations is mitigated in Short-SIT (-0.42 m), while it is -0.71 m and 0.98 m for CryoSat-2 194 and Short-SIC, respectively. Short-SIT removes ice thicker than 3 m, resulting in a lower 195 median than IceBird observations. Compared to observations from BGEP moorings (Fig-196 ure S5), the assimilation of summer CryoSat-2 SIT leads to a further underestimated SIT 197 particularly in May, but corrects the SIT overestimation in late summer. 198

SIT assimilation has an important impact on SIC simulations through the physical connection between thickness and concentration over thin ice areas (Xie et al., 2016; Mignac et al., 2022). Short-term forecast of ice edge, defined as the 15% SIC isoline, can be strongly influenced by SIT assimilation. Figure 2 shows the IIEE difference in the Pacific sector and Atlantic sector (regions shown in Figure S1). IIEE in each forecast experiment is given in Figure S6. The observed SIC used as the reference for the IIEE calculation is the NOAA/NSIDC SIC CDR. The difference in the ice-edge position between forecasts and observations in 2015 and 2016 is displayed in Figure S7 and Figure S8.

The impact of CryoSat-2 SIT assimilation on ice-edge forecasts varies with time and region. Compared to Short-CTRL, IIEE in Short-SIT is strongly reduced in most times and both sectors (Figure 2). The ice-edge position in the forecasts is consistently overestimated in Short-CTRL. Assimilation of the summer SIT reduces the SIT of the forecasts near the

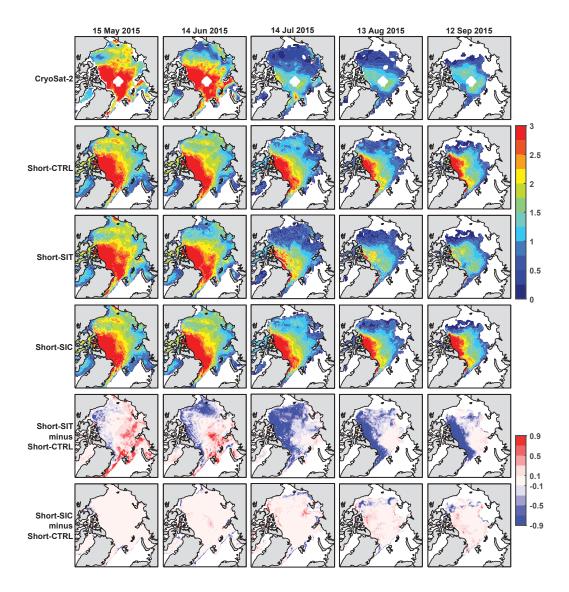


Figure 1. CryoSat-2 SIT (m) used for assimilation, SIT analysis from short-term experiments, and their differences between experiments on the 15th day from the model start date in 2015.

ice edge, resulting in a better agreement between the ice-edge forecasts and the ice-edge observations from the satellite compared with Short-CTRL (Figure S7 and Figure S8).

In the Pacific sector, only a slight improvement in IIEE is observed in May and June 213 for Short-SIT compared to Short-CTRL (Figure 2). However, in July, especially in 2015, 214 IIEE increases and the forecast skill degrades. This can be attributed to the fact that the 215 melt-pond fraction starts to increase in June and reaches its maximum in July (Feng et al., 216 2022). In particular, 2015 was the peak year for observed melt-pond fraction in the Beaufort 217 Sea between 2000-2021 (Xiong & Ren, 2023). The presence of excessive melt-pond fraction 218 in this region may lead to more misclassification of ice leads and melt ponds in the CryoSat-2 219 sea-ice freeboard retrieval using the CNN model, which affects the SIT analysis in the Pacific 220 sector. Therefore, the underestimated SIT erroneously leads to a large ice-edge error in July 221 of the Short-SIT experiments. This warrants further refinement of the artificial intelligence algorithm used for summer CryoSat-2 SIT retrieval. In late summer, the assimilation of 223 CryoSat-2 SIT observations in Short-SIT leads to more skillful ice-edge forecasts, resulting 224

²²⁵ in a statistically significant average reduction in IIEE of about 2.1×10^5 km². For example, ²²⁶ the assimilation of SIT allows the model to predict an ice-free "cave" inside the Beaufort ²²⁷ Sea in August 2015, while it is completely covered by sea ice in Short-CTRL and still with ²²⁸ a connected strip of ice in Short-SIC (Figure S7). Furthermore, the ice-edge forecasts in ²²⁹ the Atlantic sector are also improved for Short-SIT compared to Short-CTRL, especially in ²³⁰ June (about 0.8×10^5 km²) and July (more than 0.9×10^5 km²).

We further investigate the influences of SIC assimilation together with summer SIT assimilation on the ice-edge forecasts, considering the more important role of SIC observations on summer sea-ice forecasts as documented in the literature (e.g., Posey et al., 2015; Yang, Losa, Losch, Liu, et al., 2015). Forecasts from the Short-SICSIT experiments are also compared to the Short-SIC experiments, which performs SIC assimilation only.

In the Pacific sector, the additional SIT assimilation tends to yield more favorable ice-236 edge forecasts compared to Short-SIC (Figure 2). Similar to the IIEE differences between 237 Short-SIT and Short-CTRL, the improvement in May and June between Short-SICSIT and 238 Short-SIC is relatively small (only 3.0×10^3 km² on average). In July, IIEE becomes smaller 239 in 2015 but larger in 2016 relative to Short-SIC. In late summer, the analysis of summer 240 SIT observations significantly reduces the IIEE, bringing the ice-edge forecasts closer to 241 the observations. In the Atlantic Sector, Short-SICSIT tends to give rise to larger IIEE, 242 resulting in more detrimental effects, particularly noticeable in May and June (Figure 2). 243 Nevertheless, these mean IIEE differences are still in the range of $\pm 0.5 \times 10^5$ km², which is 244 much smaller than the changes between Short-SIT and Short-CTRL. In the Atlantic sector, 245 Short-SIC is already close to the observations due to a reasonable CMST SIT estimate north 246 of the Svalbard and Novaya Zemlya, so further improvements are rather limited. 247

Note that, as illustrated by the solid lines representing the mean IIEE differences in
Figure 2, the impact of the summer CryoSat-2 SIT assimilation becomes more obvious with
increasing lead time in Short-SICSIT. The improvements of Short-SICSIT relative to ShortSIC increase as forecast progressing, while the deteriorations of IIEE become smaller, with
the exception of the June 2016 forecasts.

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3.2 Long-term sea-ice forecast

The Long-SIT experiments with summer CryoSat-2 SIT assimilation provides signifi-254 cant benefits for ice-edge and thickness forecasts against Long-CTRL. Reductions in IIEE 255 are found for the first 30 days in May, June and August of 2015 and 2016 (Figure S9a, b). 256 For experiments also initialized with SIC constraints, the IIEEs are reduced for most of the 257 time during these three months, but not overall (Figure 3a, b). For the forecast initialized 258 in July, the CryoSat-2 SIT assimilation is generally detrimental and only effective for a few 259 days due to the underestimated thickness uncertainties caused by melt ponds. In Septem-260 ber, improvements in ice-edge forecasts without SIC assimilation are seen for the first three 261 weeks in 2015, and two weeks in 2016 (Figure S9a, b). The assimilation of SIC reduces such 262 benefit (Figure 3a, b), which is not surprised. 263

With respect to the CS2SMOS SIT product, the predicted Arctic-wide thickness is also 264 improved (Figure 3c, d; Figure S9c, d), except for the forecast starting in July 2016, which 265 degrades after 140 days. The summer CryoSat-2 SIT mitigates the SIT overestimation in 266 the Beaufort Sea in Long-CTRL and Long-SIC (not shown). The improvements are most 267 pronounced in October, when the freezing season begins, and decrease exponentially with 268 time until the forecast system falls into the control of the internal variability. This superior 269 skill may even persist throughout the freezing season, similar to the previous findings on an 270 optimal winter SIT initialization improving the predictive skill of summer sea ice (Blockley 271 & Peterson, 2018). Consistent with the performance of the short-term forecasts in section 272 3.1, the reduction of SIT RMSD in 2015 is more significant than that in 2016. When SIC 273 assimilation is absent, the effect of SIT initialization on ice-edge forecasts is more pronounced 274

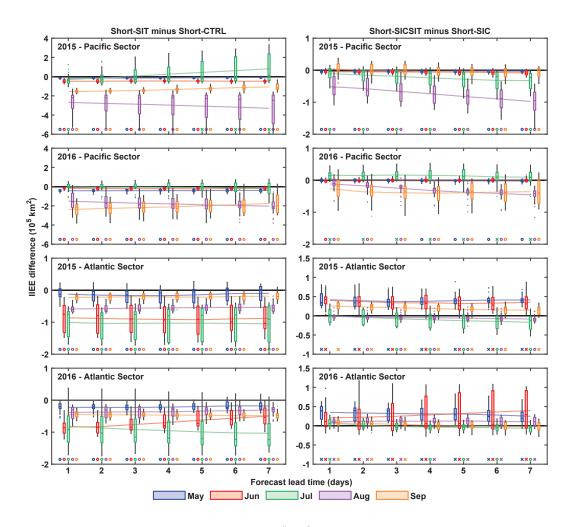


Figure 2. Box plot of the IIEE difference (10^5 km^2) between Short-SIT and Short-CTRL (left), together with that between Short-SICSIT and Short-SIC (right) in the 7-day sea-ice forecasts. The IIEE in the box plot is calculated after 7 days of assimilation when the summer CryoSat-2 SIT is fully assimilated. Box colors indicate different months. Box sizes indicate IIEE difference between the lower and upper quartiles. Outliers denote values more than 1.5 interquartile range from the top or bottom of the colored box. The outer edges of the black lines denote the minimum and maximum values that are not outliers. Solid-colored lines show the mean IIEE difference at each lead time. A positive value indicates an increase in IIEE, when SIT is assimilated, while a negative value indicates a decrease in the IIEE. Markers at the bottom of each panel indicate increases (cross) and decreases (circle) in IIEE that pass the Student's T-test at the 95% confidence level. Negative values indicate better forecast skills. Note that different subfigures use different y-axis scales.

(Figure S9). However, the skill of the long-term SIT forecasts remains nearly unchanged
 regardless of whether SIC assimilation is included.

We also examine the performance of the long-term SIT forecasts at the BGEP sites (Figure S5). In general, significant improvements in the SIT forecasts are found in Long-SICSIT initialized in July, August and September of 2015. The differences between Long-SICSIT and Long-SIC in 2016 are limited, not exceeding 30 cm most of the time. The forecasts tend to overestimate SIT in the early freezing season in the Beaufort Sea. To check

if these biases are caused by the growing errors in the long-term atmospheric forecasts, we 282 performed additional forecast experiments in 2015 with the same configuration as Long-283 CTRL, except that the CFSv2 atmospheric forecast is replaced by the ERA5 reanalysis for 284 the atmospheric forcing. The ERA5 driven simulations show a similar overestimation of 285 SIT in the Beaufort Sea (not shown). The anticyclonic wind in the Beaufort Gyre pushes 286 excessively thick ice from the multi-year ice region north of the CAA into the Beaufort Sea. 287 This suggests that the overestimation is not mainly due to biases in the atmospheric forcing 288 but imperfect model parameterizations and initial ice-ocean conditions. 289

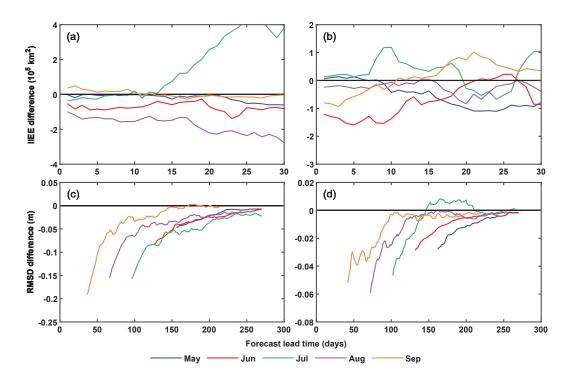


Figure 3. The difference of the IIEE (10^5 km^2) in 2015 (a) and in 2016 (b), and the difference of the SIT RMSD (m) in 2015 (c) and in 2016 (d) between Long-SICSIT and Long-SIC forecasts initialized from May to September (Long-SICSIT minus Long-SIC). The RMSD of the SIT is computed with respect to the CS2SMOS product available from October to April for (c) and (d). Negative values indicate better forecast skill. Note that different subfigures use different y-axis scales.

²⁹⁰ 4 Summary

This study examines the impact of summer CryoSat-2 SIT assimilation on short- and 291 long-term sea-ice forecasts in 2015 and in 2016. Compared to the experiments without 292 any data assimilation, the ice-edge forecasts with summer CryoSat-2 SIT assimilation are 293 improved. When the summer CryoSat-2 SIT data are assimilated together with SIC data, 294 the effects on the ice-edge forecast skill are rather dependent on the time when the forecast is 295 initialized and are spatially highly variable. In the Pacific sector, the combined assimilation 296 of summer SIT and SIC observations leads to more realistic summer ice-edge forecasts with 297 a one-week lead time. 298

The long-term sea-ice forecasts show significant reductions in both IIEE and RMSD of the SIT, except for those initialized in July, when the summer CryoSat-2 SIT has large uncertainties. The improvement in ice-edge forecasts can last up to about 30 days, while for the SIT forecasts the benefits can last for more than 3 months. This result demonstrates that, although the atmospheric forecasts used to drive the model can evolve freely after about one month, the SIT initialization in summer remains a primary factor in predicting long-term SIT variations. An extended study covering all available years of the CryoSat-2 dataset may concrete the conclusion.

However, limitations of the summer CryoSat-2 SIT data product still remain. The 307 deep learning algorithm used has a certain degree of uncertainty in classifying ice leads and 308 melt ponds, especially when the melt-pond fraction is large. The underestimation in the 309 summer CryoSat-2 SIT from July to September in the coastal regions north of the CAA and 310 Greenland requires further work on the sea-ice freeboard and thickness retrieval algorithm 311 or exploration of new correction schemes to improve their reliability and accuracy. Further-312 more, it is still an open question how this product should be used for real-time Arctic sea-ice 313 forecasting, since its uncertainty currently does not account for all the algorithm errors, and 314 possible representation errors (Janjić et al., 2018) should be considered accurately. 315

³¹⁶ 5 Open Research

The ensemble mean Arctic sea-ice thickness (SIT) and sea-ice concentration (SIC) fore-317 cast data used in the study can be downloaded at Song et al. (2024). The file size of 318 the forecast results with all ensemble members exceeds 50GB and can be made available 319 upon request through contact. The CMST SIT estimate is available at Mu et al. (2018a). 320 The summer CryoSat-2 SIT observations can be downloaded from Landy and Dawson 321 (2022). The SSMI/SSMIS SIC data is available from Kern et al. (2024). The UKMO 322 atmospheric ensemble forecasts are available in the THORPEX Interactive Grand Global 323 Ensemble (TIGGE; Bougeault et al., 2010) archive (https://apps.ecmwf.int/datasets/ 324 data/tigge). The hourly ERA5 reanalysis is available at Hersbach et al. (2023). The CFSv2 atmospheric forecasts are available at https://www.ncei.noaa.gov/products/weather 326 -climate-models/climate-forecast-system. The NOAA/NSIDC SIC CDR data is avali-327 able at Meier et al. (2021). The CS2SMOS data is available at https://www.meereisportal 328 .de. Mooring observations from BGEP are downloaded from https://www2.whoi.edu/ 329 site/beaufortgyre. The EASE-Grid Sea Ice Age, Version 4 (Tschudi et al., 2019) is 330 avaliable at https://nsidc.org/data/nsidc-0611/versions/4. 331

332 Acknowledgments

We thank two anonymous reviewers for their constructive comments. We thank Thomas 333 Krumpen for providing sea ice thickness observations from AWI IceBird campaigns. This 334 study is supported by the National Key R&D Program of China under Grant 2019YFA0607000, 335 the National Natural Science Foundation of China (42176235) and the computing resources 336 supported by the Laoshan Laboratory (LSKJ202202301, LSKJ202300303). Contribution of 337 Svetlana N. Loza was supported by the Federal Ministry of Education and Research of Ger-338 many in the framework of the Seamless Sea Ice Prediction project (SSIP, Grant 01LN1701A) 339 and partly made in the framework of the state assignment of SIO RAS (theme FMWE-2024-340 0028).341

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Figure 1.

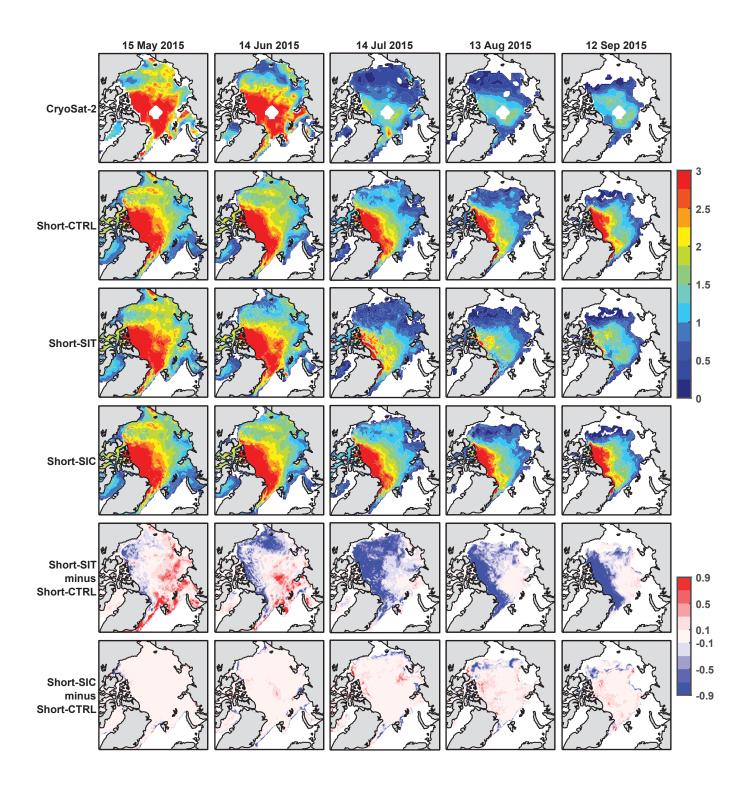


Figure 2.

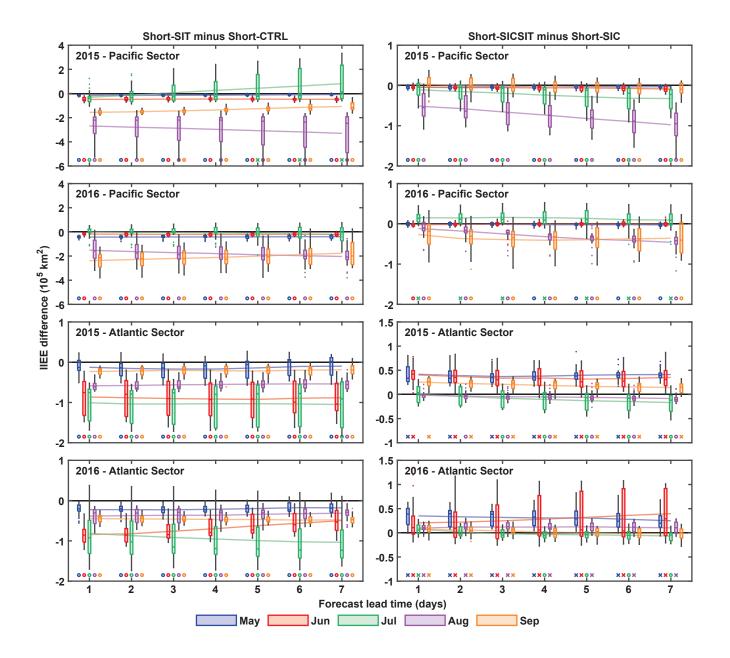


Figure 3.

