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Investigating the dynamic history of a promontory ice rise 1 using radar data 2

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ABSTRACT. Ice rises hold valuable records revealing the ice dynamics and 17 climatic history of Antarctic coastal areas from the Last Glacial Maximum to 18 today. This history is often reconstructed from isochrone radar stratigraphy 19 and simulations focusing on Raymond arch evolution beneath the divides. 20 However, this relies on complex ice-flow models where many parameters are 21 unconstrained by observations. Our study explores quad-polarimetric, phase-22 coherent radar data to enhance understanding near ice divides and domes, 23 using Hammarryggen Ice Rise (HIR) as a case study. Analysing a 5 km profile 24 intersecting the dome, we derive vertical strain rates and ice-fabric properties. 25

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These align with ice core data near the summit, increasing confidence in 26 tracing signatures from the dome to the flanks. The Raymond effect is evident, 27 correlating with surface strain rates and radar stratigraphy. Stability is inferred 28 over millennia for the saddle connecting HIR to the mainland, but dome ice-29 fabric appears relatively young compared to 2D model predictions. In a broader 30 context, quad-polarimetric measurements provide valuable insights into ice-31 flow models, particularly for anisotropic rheology. Including quad-polarimetric 32 data advances our ability to reconstruct past ice flow dynamics and climatic 33 history in ice rises. 34

35 1. INTRODUCTION

Ice rises are grounded, locally elevated, ice features surrounded by ice streams or ice shelves. They form 36 over regions with shallower bathymetry, enabling the accumulated ice to stay grounded in these areas. 37 This then results in a locally different flow regime (Matsuoka and others, 2015). Promontory ice rises, 38 such as Hammarryggen Ice Rise (HIR) (Fig. 1), are connected to the main ice sheet via a saddle in the 39 surface topography. They may form triple junctions near their domes (Fig. 1 - blue lines), from which three 40 ridges extend into the ice-rise flanks. Ice rises have two main characteristics that make them of particular 41 interest: Firstly, they decelerate ice flux from the main ice sheet towards the ocean and consequently 42 delay grounding-line retreat (Favier and others, 2012, 2014; Favier and Pattyn, 2015; Schannwell and 43 others, 2019; Henry and others, 2022). Secondly, they are an archive for the local atmospheric and 44 ice-dynamic history. The latter is accessible through the englacial stratigraphy, which includes Raymond 45 arches—anticlines in the ice stratigraphy that evolve once a local ice dome or ice divide has formed 46 (Raymond, 1983). The presence or absence of Raymond arches provides insight into the ice-rise history, 47 especially the temporal stability of the configuration, and can be used as a tie-point of the ice thickness to 48 constrain continental ice-flow models. Such tie-points are important, as other constraints, such as exposure 49 dating of rock outcrops (Davies and others, 2012), are unavailable for most of the Antarctic perimeter. 50

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52 Much progress in previous studies has guided the interpretation of observed Raymond stacks (i.e., 53 individual Raymond arches and their evolution with depth) in the context of the ice-dynamic history

of a respective catchment (Matsuoka and others, 2015). Clear signatures of transience are Raymond 54 stacks that do not align with contemporary ice divides (Nereson and Waddington, 2002), such as at Siple 55 Dome (Nereson and others, 1998). Fully evolved Raymond stacks that align with the contemporary ice 56 divide location are at the other end of the spectrum and indicate stability (e.g., Derwael Ice Rise; Drews 57 and others (2015)). Cases between these two end members (Goel and others, 2020) are more difficult 58 59 to interpret and require advanced model-data comparison, including thermomechanically-coupled full Stokes models with anisotropic rheology (Martín and others, 2009a,b; Martín and Gudmundsson, 2012) 60 and a dynamically evolving grounding line (Schannwell and others, 2019, 2020; Henry and others, 2022). 61

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A drawback of the model-guided interpretation of observed Raymond stacks is that many unconstrained 63 factors influence the arch amplitude. One of them being the ice anisotropy (Martín and Gudmundsson, 64 2012; Drews and others, 2015) for which so far virtually no observations away from ice cores were 65 available. This is the main problem that we address in this paper using polarimetric radar as a main 66 tool. Arch amplitude is influenced by multiple interrelated factors that affect the development of ice 67 fabric. Firstly, the degree of non-linearity in Glen's flow law exponent significantly impacts arch size; a 68 higher non-linearity typically results in larger arch amplitudes (Gillet-Chaulet and others, 2011; Martín 69 and others, 2009a,b; Drews and others, 2015; Bons and others, 2018). In contrast, the along-ridge flow 70 component generally produces smaller arches (Martín and others, 2009a,b). Similarly, variations in bed 71 topography can lead to smaller arches when the bed is uneven (Kingslake and others, 2014), while basal 72 sliding also contributes to reduced arch sizes (Petit and others, 2003). Additionally, localized factors 73 such as surface mass balance and erosion at the crest can increase arch amplitudes (Drews and others, 74 2015; Conway and Wilbour, 1999). The historical thinning or thickening of the ice further translates to 75 changes in arch sizes relative to their current geometry (Martín and others, 2006; Goel and others, 2018). 76 77

Ice-core analysis, in combination with shallow and deep radar, can constrain the three-dimensional ice geometry (Hindmarsh and others, 2011) and the surface accumulation history (Philippe and others, 2016; Goel and others, 2017; Cavitte and others, 2022). Strain measurements such as the coffee-can method (Hamilton and Whillans, 2000) and repeat surveys with phase-coherent radar can provide additional constraints on the vertical strain rates (Kingslake and others, 2014). However, other factors, such as ice anisotropy, remain unconstrained, resulting in ambiguous matching of observed Raymond arch stacks with ice-flow models (Drews and others, 2015). Consequently, so far, ice rises and their inferred
dynamic history play a minor role in constraining larger-scale ice flow models (Bentley and others, 2014).

Phase coherent radar polarimetry using a ground-based phase-sensitive Radio Echo Sounder (pRES) 87 (Brennan and others, 2014) has seen much development in terms of inferring ice-fabric types for 88 89 various flow regimes using the polarimetric coherence phase as a metric to extract information from the birefringent radar backscatter (Dall, 2010; Jordan and others, 2019, 2020; Ershadi and 90 others, 2022; Rathmann and others, 2022; Zeising and others, 2023). Anisotropic ice-flow models 91 of steady-state ice rises, as detailed in studies by Martín and others (2009a,b); Martín and 92 Gudmundsson (2012), predict significant gradients in ice-fabric types on either side of an ice divide. 93 This prediction, highlights the impact of anisotropic rheology on ice dynamics. However, thus far, 94 it has not been directly compared with observations, a gap that warrants attention in the field. 95 96

97 Here, we investigate to what extent ice-fabric properties can be derived from quad-polarimetric radar data 98 near a triple junction of HIR in Dronning Maud Land, East Antarctica. We validate the inferred ice-fabric 99 types with ice-core data near the summit and provide additional context in terms of variability in vertical 100 strain rates and corresponding signatures in the radar stratigraphy.

101 2. STUDY AREA & DATA

HIR is a promontory ice rise located in eastern Dronning Maud Land (Fig. 1). It has a discernible dome at 102 367 meters above sea level (m a.s.l.) (Howat and others, 2022) that is co-located with a triple junction from 103 which three ridge divides extend into the ice-rise flanks. The ice thickness at the dome is approximately 104 550 m (Fig. A1). The average accumulation rate and mean ice thickness within the 5 km pRES profile 105 are reported as 0.4 m a^{-1} (Cavitte and others, 2022) and 550 m, respectively. The ratio of both values 106 (thickness/accumulation) provides a characteristic time scale (t_D) , which is a reference of the time it takes 107 for a change to advert through the system (Martín and others, 2009a). For HIR, t_D is approximately 1400 108 years. In this study we use three different dataset collected at HIR. 109

Phase coherent radar data: In 2019, 15 static, quad-polarimetric measurements were taken along a 5 km profile crossing the triple junction HIR in northwest-to-southeast direction (Fig. 1b - red line). At each site, we infer the magnitude and the orientation of ice fabric with depth (sect. 3.1). One static measurement (site name p0) was taken at a few tens of metres distance from the ice core, which validates our inference



Figure 1: (a) The location of study area in Antarctica. (b) Hammarryggen ice rise, the white contour lines and satellite background represents the surface elevation derived from the REMA dataset (Howat and others, 2022). Two black dashed lines represent the UWB flight lines. The blue lines denote the approximate position of the ridges. The black dot represents the location of the ice core and, the red line indicates the pRES profile. (c) The red shading corresponds to the location of the pRES profile. pRES measurement points depicted as red dots in the inset. (d) and (e) A cross-sectional view along the extended pp' profile, illustrating surface elevation (Howat and others, 2022), bed elevation and ice thickness (Morlighem, 2022).

with values derived from ice-core data (sect. 3.2). In 2020, all static sites were revisited to determine theyearly-averaged vertical strain rates (sect. 3.3).

Airborne radar data: The airborne radar data were collected in December 2018 and January 2019 as part of CHIRP (Channel and Ice Rise Project; Jansen and others, in: Fromm and others (2019)) using the ultra-wideband radar system (UWB) of the Alfred-Wegener-Institut Helmholtz-Zentrum für Polar- und Meeresforschung (2016) with a frequency range of 150-520 MHz. The system was deployed to survey the area providing ice thickness and internal ice stratigraphy data (sect. 3.4) at multiple cross sections roughly oriented along the East-West direction (Fig. 1b - black dashed lines).

Ice core fabric data: During the 2018-2019 austral summer field season, a 263 m long ice core was drilled at the summit of HIR (70.49960°S, 21.88019°E) (Fig. 1b - black dot). The ice core provided the age-depth relationship used to date near-surface radar stratigraphy imaged with a different ground-based radar in order to extrapolate the surface mass balance spatially (Cavitte and others, 2022). The ice core



Figure 2: A cross-sectional view along the extended pp' profile (Fig. 1), illustrating (a) surface velocity (Shallow-ice approximation and Rignot and others (2017)), and (b) surface mass balance (Lenaerts and others, 2014; Cavitte and others, 2022). The red shading corresponds to the location of the pRES profile.

126 was also analyzed to investigate ice crystal fabric. In this study we will only use the ice core fabric data to 127 verify inferences drawn from 15 quad-polarimetric radar observations.

This publication marks the first release of all the data presented here, with the exception of the AA' UWB profile (illustrated by the black dashed lines in figure 1b), which was previously published by Koch and others (2023a). Additionally, an approximation of surface velocities and corresponding horizontal strain rates based on the shallow ice approximation (SIA) (sect. 3.5) is provided.

132 **3. METHODS**

133 3.1. Ice-fabric derived from static, phase-coherent radar

Propagation of radio waves through ice is polarization dependent because ice is mechanically and dielectrically anisotropic (Hargreaves, 1977, 1978; Fujita and others, 2006). More specifically, radio wave speed depends on the orientation of the ice crystals relative to the radio-wave polarization which leads to variability in backscattered power (through birefringence and anisotropic reflections) as a function of antenna orientation at the surface. The degree and type of anisotropy in ice, in short the ice-fabric type, is often described using three eigenvectors $(\vec{v}_1, \vec{v}_2, \vec{v}_3)$ and eigenvalues $(\lambda_1, \lambda_2, \lambda_3 \text{ with } \lambda_1 < \lambda_2 < \lambda_3$ and $\lambda_1 + \lambda_2 + \lambda_3 = 1$) which correspond to an ellipsoid best describing the bulk orientation of individual

crystal c-axis at a given depth. The directions are locally defined, but can be georeferenced using the 141 antenna orientation at the surface. Inferring the anisotropic ice properties from polarimetric radar data 142 has been the subject of many previous studies (Dall, 2010; Jordan and others, 2019, 2020; Ershadi and 143 others, 2022; Zeising and others, 2023) and some consensus has emerged that the polarization dependence 144 145 can be fully captured using a quad-polarimetric setup in which four antennas are oriented perpendicuarily 146 to each other (?Ershadi and others, 2022, 2024). Following the notation from the satellite remote sensing literature, the two orthogonal polarizations are referred to as horizontal (H) and vertical (V), although they 147 are both situated in the horizontal plane. Each quad-polarimetric measurement consists of four individual 148 measurements with co-polarized (HH, VV) and cross-polarized (HV, VH) orientations. The data can be 149 synthesized to mimic a full azimuthal orientation of the antennas, and variations in backscatter power are 150 displayed correspondingly (Young and others, 2021; Ershadi and others, 2022, 2024). 151

Here, the quad-polarimetric data (Pattyn and others, 2023) at each site were collected with a fixed 152 antenna distance (5 m between centres), and the absolute, georeferenced orientation of the baseline 153 connecting the two antennas is determined with a compass with approximately 15° uncertainty. We 154 determine the horizontal ice fabric anisotropy $(\Delta \lambda_H = \lambda_2 - \lambda_1)$ and its georeferenced orientation as 155 the direction of the strongest horizontal eigenvector (\vec{v}_2) using a polarimetric forward model (Fujita 156 and others, 2006) and an and inversion outlined in Ershadi and others (2022). This method employs 157 HH and HV power anomaly data and the HHVV coherence phase, defined as the argument of the 158 complex polarimetric coherence and its scaled phase derivative, which estimates the depth variability of 159 $\Delta \lambda_H$ and \vec{v}_2 assuming that one (in this case \vec{v}_3) of the eigenvectors is pointing vertically. Additionally, 160 the method allows for the estimation of all three eigenvalues assuming that ice is isotropic at the 161 surface. This enables the reconstruction of the vertical anisotropy $(\Delta \lambda_V = \lambda_3 - \lambda_2)$ in a top-to-162 bottom approach. In this case a weak $\Delta \lambda_H$ would be reflected in a smoothly varying coherence phase. 163 A strong $\Delta \lambda_H$, on the other hand, would result in multiple nodes where the coherence phase is 164 wrapped at the 2π boundaries. For HIR specifically, we limit our analysis to a magnitude of coherence 165 of 0.4 following recommendations from Jordan and others (2019). This covers approximately the 166 upper 400 m, corresponding to approximately 70 % of the total ice thickness near the dome (Fig. A1). 167 168

To categorize the various observed ice fabric types and their development at different depths, we employ a classification method that uses the logarithmic ratios of the eigenvalues. This approach effectively distinguishes between cluster-type (point maximum) and girdle-type fabrics, as outlined by Woodcock (1977). The key parameters in this scheme are $K = \frac{\ln(\lambda_3/\lambda_2)}{\ln(\lambda_2/\lambda_1)}$ and $C = \ln(\lambda_3/\lambda_1)$, where K serves to identify whether the fabric is a uniaxial girdle or cluster, and C measures the intensity of the identified ice fabric type. K and C are later referred to as "Woodcock parameters". The evolution of fabric types in relation to flow regimes is well described by Llorens and others (2022) providing comprehensive models and visual representations that elucidate the relationship between ice deformation and the resultant fabric patterns.

177 3.2. Ice-fabric from ice-core data

The ice core was cut in 0.5 m sections on site, then packed, transported to and stored at the Laboratoire de Glaciologie (Université libre de Bruxelles (ULB), Belgium) respecting the cold chain (temperature below -25°C) at all times. Dating and interpretation of a series of environmental and climatic proxies for the upper 120 metres of the core are beyond the scope of this paper and are presented separately in Wauthy and others (2024). Here we will focus on the icefabric properties of the entire ice core, more specifically the eigenvalues of the eigenvectors, characterizing the ice-fabric anisotropy that we aim to reconstruct from the pRES measurements.

To determine the eigenvalues of the ice fabric from the ice core, 114 regularly spaced 8 cm high and 500 186 μ m thick vertical thin sections of ice were produced following the standard procedure of Langway (1958). 187 The thickness of the ice core sections, typically between 500 μ m and 600 μ m, ensures that there is no 188 superposition of crystals, allowing for accurate 3D fabric analysis. The Automatic Fabric Analyzer effectively 189 measures the orientation of individual pixels and uses image analysis to determine grain boundaries and 190 calculate the mean orientation within each grain, providing robust data for deriving eigenvectors. Crystal 191 (optic) c-axes orientations were measured using the G-50 Automated Ice Fabric Analyzer (Russell-Head 192 Instruments, e.g., Wilson and others (2003)). Eigenvectors and eigenvalues were calculated using the FAME 193 software (Hammes and Peternell, 2016). The same software was used to determine grain boundaries, to plot 194 c-axis orientation density distributions in a lower hemisphere, equal-area or Schmidt diagram. Schmidt 195 196 diagrams are a common representation in geology providing equi-areal 2D projections of the ice crystal's c-axes intersection with a lower hemisphere into the equatorial plane, chosen in the plane of the vertical 197 thin sections in this study. Density diagrams are constructed by counting the number of c-axes falling in a 198 reference counting circle displaced on a regular grid across the Schmidt diagram. 199

200 3.3. Vertical strain rate

The sites used for the polarimetric surveys (sect. 3.1) were marked with bamboo stakes and revisited one year later. The phase-coherent repeat measurements enable tracking of the submergence of internal reflections relative to the bed (Kingslake and others, 2014). This allows us to infer yearly averaged vertical strain rates, a method which is commonly applied to ice shelves in order to isolate the basal melt rate signal from observed thickness change (e.g., Nicholls and others (2015); Sun and others (2019)). For HIR specifically, we calculated depth-averaged values of vertical strain rate for ice thickness intervals over tens of metres in order to highlight signatures of the Raymond effect.

208 3.4. Airborne radar data

The UWB radar is an improved version of the Multichannel Coherent Radar Depth Sounder (MCoRDS 209 5) developed at the University of Kansas, Center for Remote Sensing and Integrated Systems (Rodriguez-210 Morales and others, 2014; CReSIS, 2021), operated on AWI's Polar6 BT-67 aircraft (Alfred-Wegener-Institut 211 Helmholtz-Zentrum für Polar- und Meeresforschung, 2016). The radar system consists of an eight-element 212 antenna array polarized in HH, which serves as a transmitter and receiver unit for radar signals. Data 213 acquisition and processing methods are detailed in Koch and others (2023a) and are similar to those 214 described by Franke and others (2021) and Franke and others (2022). During CHIRP, the radar transmitted 215 three-stage linear modulated chirp signals (1 μ s low-gain, 1 μ s high-gain and 3 μ s high-gain to sound the 216 upper, middle and deeper part of the ice column in high quality) in a frequency range of 150-520 MHz 217 and at an acquisition height of ~ 360 m above the ice surface. Radar data processing was conducted with 218 the CReSIS Toolbox (CReSIS, 2021) and comprises pulse compression, synthetic aperture radar (SAR) 219 processing with a wide angular range, and array processing (Rodriguez-Morales and others, 2014; Hale and 220 others, 2016; Franke and others, 2022). The processed radar data have a range resolution of ~ 0.35 m and 221 an along-track trace spacing of approximately 6 m. Here, we use selected sections of the airborne radar data 222 to analyze signatures of the Raymond arches beneath the dome and the landward-oriented ice divide (Fig. 223 1). 224

3.5. Shallow ice approximation: surface velocities and strain rates

Surface velocities at HIR are too low to be reliably measured up by remote sensing data. Therefore, we use the shallow-ice approximation (SIA; Hutter (1983); Greve and Blatter (2009)) as a rough estimate of the surface velocity and maximum horizontal strain rate ($\dot{\varepsilon}_{max}$), whilst being aware that a higher-order ice flow model would be more accurate in the region. We use the calculated surface flow direction and the maximum strain rate direction, $\dot{\varepsilon}_{max}$, to compare with the estimated strongest horizontal anisotropy eigenvector, \vec{v}_2 . The map of HIR with the estimated magnitude and orientation of the surface velocity and maximum horizontal strain rate is shown in Appendix D.

Our calculation of velocities using SIA is not without uncertainty. Although bed elevation errors in BedMachine data are relatively low at Hammarryggen Ice Rise, there are some error estimates of up to 100 m on the southern side of the ice rise away from the radar profile (Morlighem and others, 2020). Furthermore, we have made the assumption that ice is isothermal, but given that we are most interested in comparing strain rate directions with the observational anisotropy data rather than strain rate magnitudes, errors due to this assumption are likely to be small.

239 4. **RESULTS**

4.1. Inference of ice-fabric parameters from pRES measurements

We use the pRES measurement site closest to the ice-core site (marked p0 in figure 1) to illustrate results 241 from the quad-polarimetric analysis. The observations from the quad-polarimetric measurements are 242 displayed using multiple metrics. The HH power anomaly (Fig. 3a) represents the backscatter dependence 243 as a function of antenna orientation and is indicative of anisotropic reflections, e.g., due to vertical 244 variability in ice-fabric strength. The HHVV coherence phase (Fig. 3b) shows the phase correlation 245 between the HH and VV directions. Stronger vertical gradients correspond to a stronger $\Delta \lambda_H$. The HV 246 power anomaly (Fig. 3c) is an analogue to the HH power anomaly but for the depolarization component 247 and is a proxy for the ice-fabric orientation (marked with green dots). The scaled phase derivative 248 (Fig. 3d) of the ice-fabric orientation for a given depth interval (marked with green dots) is defined as 249 $\Delta \lambda_{H}$. Figure 3e-f show the same metrics based on a radio-wave propagation model (Fujita and others, 250 2006) and ice-fabric parameters resulting from a non-linear optimization method (Ershadi and others, 2022). 251

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The characteristic signatures (e.g., nodes, location of maxima, etc.) in the observations (Fig. 3a-d) are well reproduced by the optimized forward model output (Fig. 3e-h) demonstrating that the inferred icefabric eigenvalues and their changes with depth are adequately captured by the inversion. The gradient in the polarimetric phase coherence indicates a gradual strengthening of $\Delta \lambda_H$ with depth (Fig. 3d), and the minima in the HV power anomaly suggest that the ice-fabric orientation changes are small with depth



Figure 3: Results for the p0 radar site: (a) to (d) pRES observations, with green dots in (c) and (d) marking the minima in PHV. (e) to (h) Optimized model output capturing the principal patterns of the observations.

(Fig. 3b). An exception occurs in the depth interval between 150 and 200 m, where a cross-polarization extinction node suggests a rotation of the \vec{v}_2 eigenvector of several degrees (Fig. 3c,g). We first substantiate the inferred ice-fabric parameters from the radar polarimetry by comparing them to ice-core measurements in the following section, and then continue by tracing the ice-fabric parameters away from the ice core into the ice-rise flanks.

263 4.2. Ice core validation

The fabric data measured from ice core samples show an increase with depth of λ_3 and a decrease of 264 both λ_1 and λ_2 (Fig. 4). The measured $\Delta \lambda_H$ indicates a weak horizontal anisotropy within the ice 265 column and remains almost constant with depth. In contrast the measured $\Delta \lambda_V$ increases with depth. 266 This behavior of eigenvalues results in Woodcock parameters K > 1 and C < 2, categorizing the fabric 267 type into a weak uniaxial cluster. This pattern (increasing areal concentration of crystals' c-axes from 268 white to red) is evident in the density Schmidt diagrams (Fig. 4c), which are directly measured from 269 the ice core. Additionally, figure C1 allows for a better comparison between the observed and estimated 270 fabric types, demonstrating that the fabric is nearly isotropic and evolves towards a weak uniaxial cluster. 271

The estimated eigenvalues from the quad-polarimetric radar measurement at site p0 are compared 273 with the measured ice-core eigenvalues (Fig. 4). The estimated eigenvalues and anisotropy in both 274 the horizontal and vertical directions exhibit the same behavior as the measured ones. However 275 the estimated λ_1 and λ_2 (Fig. 4a) are about 0.07 and 0.03 larger than the measured values, 276 277 respectively, and consequently, the estimated λ_3 is systematically smaller than the measured value. 278 Both estimated and measured $\Delta \lambda_H$ are weak (approximately 5 % of the maximum possible horizontal anisotropy $\Delta \lambda_H = 1$ (Fig. 4b), with the estimated one being slightly weaker than the measured 279 one). In contrast, both the estimated and measured vertical ice fabric anisotropy $\Delta \lambda_V$ increase 280 with depth (Fig. 4c). Similar to $\Delta \lambda_H$, the estimated $\Delta \lambda_V$ is also weaker than the measured $\Delta \lambda_V$. 281 282

Similarly to the ice core data, the radar-derived fabric shows a tendency to form clusters which increase in 283 strength with increasing depth (Fig. 4c). The differences seen in the eigenvalue magnitudes correspondingly 284 translate into the K and C classification: The estimated C values (color of marks in figure 4c) are weaker 285 than the measured ones, particularly on the shallower part of the ice column. The minimum C value 286 estimated from radar at site p0 is 0.19, and the maximum is 1.81. In contrast, the ice core values are 0.36 287 and 2.35, respectively. The estimated $\Delta \lambda_H$ between 350 and 380 increases to 0.12 (Fig. 4b), resulting from 288 the corresponding change in λ_1 and λ_2 (Fig. 4a). This behavior does not affect $\Delta \lambda_V$ (Fig. 4c), but it does 289 affect the K value (Fig. 4c) which is close to unity. However, no ice-core data are available at that depth 290 to validate this behavior. It is important to note that figure 4c shows a limited range of fabric types, while 291 figure C1 in the appendix provides a fuller context for better comparison between measured and estimated 292 fabric. Although the fabric type is broadly captured, its depth variability is overestimated by the pRES data. 293 This overestimation stems from systematically low horizontal anisotropy values (Fig. 4b - blue line), which 294 295 are disproportionally amplified because the low horizontal anisotropy values appear in the denominator of K. 296

4.3. Spatial changes in ice-fabric and vertical strain rates along the 5 km transect

After comparing the consistency between the estimated eigenvalues derived from polarimetric radar data at the p0 site and the measured ice core eigenvalues, we reconstruct ice-fabrics for all sites p1 to p14 along the 5 km long transect. To interpret our results, we normalize distances and elevation with the ice thickness at the dome ($H \simeq 550$ m). The distance of the pRES points from the dome denoted as X is normalized as x = X/H. Additionally, elevation is expressed as the normalized ice height above the bed, denoted as



Figure 4: Comparison between estimated and measured (a) eigenvalues, (b) horizontal and vertical ice fabric anisotropy as $\Delta \lambda_H$ and $\Delta \lambda_V$, respectively and (c) Woodcock values K and C with density Schmidt diagrams measured from the ice core. Note that the estimated values are the results from the inverted radar data, and the measured values are from the ice-core laboratory analysis.

z = (H - Z)/H, where Z represents the depth. In this context, the mean bed elevation and mean surface elevation along the pRES profile are designated as z = 0 and z = 1, respectively. Subsequently, we employ linear interpolation to obtain the spatial variation of the fabric parameters along the 2D transect (Fig. B1).

Depth-averaged values of the horizontal anisotropy $\Delta \lambda_H$ show differences on both sides of the divide 307 (Fig. B1a). On the south-eastern side, where ice is thicker, values of $\Delta \lambda_H$ are in general larger and more 308 variable than on the north-western side. In the 30-35 % depth-interval , the averaged $\Delta\lambda_H$ exhibits a 309 local maximum beneath the summit that is approximately one ice thickness wide and is asymmetrical. The 310 north-western side also exhibits slightly smaller maxima beneath the ice-rise flanks. The spatial distribution 311 of the magnitude of the strongest estimated eigenvector λ_3 (Fig. B1b) exhibits a similar pattern in terms 312 of a local maximum beneath the divide and has generally larger values on the north-western side. The 313 depth-average orientation of \vec{v}_2 , aligns within 10° with the North-South direction (Fig. B1c). This direction 314



Figure 5: (a) Depth-averaged variation of $\Delta \lambda_H$ within a specific depth window. (b) Depth-averaged variation of λ_3 within a specific depth window. (c) Depth-averaged horizontal ice fabric orientation (blue line), surface flow direction derived from SIA (dashed red), and maximum strain direction derived from SIA (red line). (d) Vertical strain rates measured at each pRES site averaged over different depth intervals. Note that more negative strain rates indicate stronger deformation. The x-axis is the distance from the dome normalized by H.

is ~ 40° offset to the mean flow direction in the ice-rise flanks and ~ 81° offset to the direction of maximum horizontal strain inferred from the SIA-based velocity field. The magnitude of the depth-averaged vertical strain rates (Fig. B1d) is highest in the top 20° of the ice thickness (80 to 100° depth interval), where the densification of firm is strongest. Vertical strain rates are also overall smaller in absolute value in the thinner north-western flank than the thicker south-eastern flank. At approximately 50° of the ice thickness, the vertical strain rates exhibit a pronounced (weakly double-peaked) minima beneath the divide which extends laterally for 1-2 ice thickness into the ice-rise flanks.

322 4.4. Internal stratigraphy

The airborne UWB radar profiles (Fig. 6) image ice thickness and internal radar stratigraphy in profiles 323 located nearly perpendicular to the local ice divides (Fig. 1). The average ice thickness is between 500 and 324 600 m beneath the divides. The bed increases in elevation towards the west and deepens from the triple 325 junction into the landward direction. The bed beneath the saddle (Profile B-B') appears distinctly rougher 326 than beneath the dome area (Profile A-A'). The internal radar stratigraphy is clearly visible in both profiles 327 but cannot be identified unambiguously at depths deeper than the surface multiple (Koch and others, 328 2023a). Continuous tracking of the stratigraphy is also difficult in areas where internal layers are more 329 inclined (i.e., near the divides) (Holschuh and others, 2014), and in areas where the flight track is curved (Fig. 330 1). Nevertheless, internal radar stratigraphy close to the surface appear deeper in the south-eastern flanks 331 compared to the north-western flanks, and their syncline arching beneath the divide is clearly visible in B-B' 332 (i.e., beneath the saddle) and to a lesser extent also along A-A' (just north-west of the dome). The arches 333 increase in amplitude with increasing depth and are vertically aligned with today's divide position (Fig. 1). 334 335

336 5. DISCUSSION

Previous studies have investigated ice-rise evolution using flow-line modeling in combination with the internal isochronal radar stratigraphy as principal observations (Drews and others, 2013, 2015; Goel and others, 2017, 2018; Martín and others, 2009a,b; Martín and Gudmundsson, 2012; Hindmarsh and others, 2011). Two additional studies of a dome and ice rise, respectively, used the observed vertical strain rates (Gillet-Chaulet and others, 2011; Kingslake and others, 2014). Here we use all of the previous observations and add quad-polarimetric radar measurement as another possible observational constraint. We now investigate whether those observations capture signatures of the Raymond effect and, if so, how these



Figure 6: Airborne UWB radargrams crossing two ridges of the triple junction dome (A-A') and the saddle ridge (B-B'). Red curves highlight laterally coherent internal reflection horizons, and red dashed lines contain in parts data gaps, particularly in areas where the layers are more inclined.

can be contextualized with other geophysical observations of the contemporary flow regime. This may guide the application of a future 3D model (incl. thermo-mechanical coupling and anisotropic rheology) which is capable of simulating the complex dynamics occurring at triple junction ice rises. Given that the extraction of ice-fabric parameters from quad-polarimetric data using non-linear inversion has so far only once been compared with direct ice-core measurements (Ershadi and others, 2022), we first discuss the benefits and limitations of this method in general before moving on to investigate the flow history of HIR.

³⁵⁰ 5.1. Applicability of the inferred the ice-fabric eigenvalues

The quad-polarimetric analysis has a limitation in that it assumes one of the principal eigenvectors 351 points upwards. Although this assumption can be relaxed (Rathmann and others, 2022), it leads to a 352 more complicated forward model for which the inversion is not yet established. However, (Rathmann and 353 others, 2022) show that the polarimetric radar response of nadir-looking radars is comparatively insensitive 354 355 to ice fabrics that are vertically tilted. However, beneath ice domes vertical compression is assumed to dominate, which is expected to lead to a vertical point maximum in the c-axes distribution (Budd and 356 Jacka, 1989; Llorens and others, 2022) We, therefore, consider the assumption of horizontal and vertical 357 eigenvectors to be justified, and not likely a cause for the systematic mismatch in magnitude that we 358

observe between the eigenvalues from the quad-polarimetric method and the ice-core-based values (Fig. 4a).

The systematic underestimation of $\Delta \lambda_H$ and $\Delta \lambda_V$ compared to ice-core values has to a lesser extent 361 also been observed at the ice-core site of the European Project for Ice Coring in Antarctica (EPICA) at 362 363 Concordia Dome C (EDC), however, it does not occur at the EPICA site in Dronning Maud Land (EDML) 364 (Ershadi and others, 2022). We investigated if using a scaling factor to the dielectric anisotropy for a single 365 crystal (commonly assumed to be 0.034 (Matsuoka and others, 1997)) can explain the underestimation. However, the mismatch did not significantly improve when changing dielectric anisotropy within the reported 366 uncertainties. The inversion is also sensitive to the fabric orientation and backscatter ratio. The latter in 367 turn varies according to the ice-core data on shorter spatial scales than what the inversion can currently 368 resolve, particularly because it involves vertical averaging to smooth the phase gradient. The reason for the 369 underestimation of $\Delta \lambda_H$ and $\Delta \lambda_V$ therefore requires further investigation, but given that the gradients are 370 well reproduced, this does not hinder the interpretation of lateral ice-fabric variability. 371

372 5.2. pRES detects geo-referenced fabric orientation

The estimated \vec{v}_2 , as depicted in figure 5c, is derived solely from pRES data, without validation from field datasets. To overcome this limitation, we used surface flow direction data obtained from SIA modeling to compute the eigenvectors and eigenvalues of the strain rate tensor $\dot{\varepsilon}$. When comparing \vec{v}_2 to the surface flow direction, a deviation of ~ 40° is observed (Fig. 5c blue vs. dashed red). In contrast, when compared to the direction of maximum horizontal strain rate, \vec{v}_2 shows a deviation of ~ 81° (Fig. 5c blue vs. solid red).

It is established by Alley (1992) that during ice deformation, c-axes consistently rotate towards 379 compressional axes and away from tensional axes. Also, the principles of fabric orientation under vertical 380 shortening is discussed by Passchier (1997) where the theory explains that basal planes rotate towards 381 the horizontal plane, which serves as the fabric attractor. Consequently, the perpendicular c-axes rotate 382 towards the vertical direction. The rotation is most rapid in the plane containing the direction of maximum 383 shortening (vertical) and maximum stretching. As a result, the variation in the horizontal c-axes, described 384 385 by λ_1 in the direction \vec{v}_1 , is narrowest in this plane. \vec{v}_2 is perpendicular to this direction in the horizontal plane, hence it is expected to be oriented at 90° to the direction of maximum stretching, which indeed 386 corresponds to our observations in figure 5c (~ 81°). Also, as suggested by the pRES measurements, λ_1 387 and λ_2 exhibit similar intensities (weak $\Delta \lambda_H$), it follows that the same might hold true for $\dot{\varepsilon}_1$ and $\dot{\varepsilon}_2$. 388

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Their combination would then yield maximum horizontal strain at approximately 45° from \vec{v}_1 and \vec{v}_2 . This explains why \vec{v}_2 appears at approximately 45° from the flow direction in figure 5c (~ 40°).

³⁹¹ 5.3. Synthesis of radar observations within the ice-dynamic setting of HIR

The radar stratigraphy, the strain rates and the ice-fabric properties are all jointly influenced by the ice-dynamic evolution of HIR and encode parts of its history, even though it is not yet clear how rapidly ice-fabric parameters change with the ice-dynamic flow regime. Here we synthesize the different datasets with a particular focus on the Raymond effect and contextualize our findings with available modeling and observational studies of other ice rises.

The upward arches observed beneath the saddle (Fig. 6, B-B' flight line) are typical of ice rises in 398 the sense that they are located beneath today's divides and that they are asymmetrical in shape. For 399 example, a syncline as on the western side has also been observed at Derwael Ice Rise and explained 400 with persistent accumulation patterns including erosion of snow at the crest and re-deposition in 401 the flanks (Drews and others, 2015). Erosion of snow at the crest increases the amplitudes of the 402 upward arches at larger depths which are, however, primarily formed by the Raymond effect. Both 403 mechanisms require a stable ridge divide position and therefore testify that the saddle connecting 404 HIR with the main ice sheet was stationary, probably for several t_D , i.e., several thousands of years. 405 Upward arching also occurs beneath the dome (Fig. 6, at kilometer 10 in profile A-A'), but the 406 amplitudes are smaller compared to the saddle. The eastern side of A-A' is near-parallel to the eastern 407 arm of the triple junction and hence strong upward arching is not expected in the stratigraphy here. 408 It is therefore unclear if the triple junction of HIR exhibits a Raymond cupola as modeling would 409 suggest (Hindmarsh and others, 2011), but if it does, the lower arch amplitudes could suggest that 410 the dome position is younger than the saddle, although three-dimensional effects may be responsible. 411 412

For a two-dimensional, plane strain flow regime, it is well understood that lateral differences in vertical velocities that accompany the formation of Raymond arches, are expressed by corresponding patterns in the vertical strain rates. More specifically, the vertical strain rates are expected to be smaller in magnitude for 100 to 300 m depths (z from ~ 0.8 to 0.5) beneath the divide compared to the flanks (Kingslake and others, 2014). Our observations (Fig. 5d) comply with these predictions, particularly for 330 to 380 m depths (z from ~ 0.4 to 0.3). At shallow depths (top 100 m) the vertical strain rates are

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dominated by firn compaction, and deeper depth intervals could not be resolved. Observed magnitudes of 419 approximately 1.0×10^{-3} m a⁻¹ are comparable to what has been observed at other triple junctions (i.e., 420 Fletcher Promontory (Kingslake and others, 2014)), although the amplitude of the vertical strain rate 421 anomaly across the dome is smaller. Once a local divide or dome has formed, the effect on the velocity 422 423 field is instantaneous, and hence the vertical strain rates do not contain information about the ice-rise 424 history per se. However, ice-fabric types are strain-induced and develop over time (Budd and Jacka, 1989). Consequently, if the dome position was temporally stable, corresponding signatures should appear in the 425 derived ice-fabric types from the quad-polarimetric analysis, indicating a temporarily stable dynamic regime. 426

Regarding the ice fabric, below 150 m where the distribution of the orientation of the fabric slowly 428 (low values on the density scale) evolves from a more random distribution in the top of the ice core 429 towards a single maximum closely centred on the vertical as expected from dominant uniaxial compression 430 at ice domes (e.g., Durand and others (2007)). The gradual strengthening of the fabric anisotropy is 431 clearly seen in the evolution of the measured eigenvalues (Fig. 4a). The small but increasing horizontal 432 anisotropy (Fig. 4b), indicating that the strain is not purely uniaxial flattening (compaction) but includes 433 differential deformation (such as lateral extension) in the horizontal plane which is coherent with the 434 complexity of the geomorphological setting (triple junction). The ice-fabric reconstruction from the 435 quad-polarimetric data shows that minima in the vertical strain rates (Fig. 5d) are accompanied by 436 corresponding maxima in $\Delta \lambda_H$ and λ_3 (Fig. 5a,b) in 330 to 380 m depth interval (z from ~ 0.4 to 0.3). 437 This is in line with measured ice fabric and two-dimensional model predictions of Martín and others 438 (2009a) which predicts a single maximum fabric which is stronger beneath the divide compared to the flanks. 439 440

441 A quantitative comparison in terms of timing between our observations and the model predictions of Martín and others (2009a) is hampered in several ways: first, the assumed two-dimensional geometry 442 does not include the triple junction geometry of HIR, and second, the model predictions assume 443 an evolution from fully isotropic to fully anisotropic ice. The latter is unlikely to be the case for 444 HIR as demonstrated by the measured ice fabric data. Notwithstanding, in steady-state (i.e., at 445 approximately 10 times t_D) the predicted degree in ice-fabric anisotropy is larger than what is 446 reconstructed from quad-polarimetric data here. The reconstructed $\Delta \lambda_H$ consistently remains below 447 0.1 which is comparable to other domes such as Dome C, but is much weaker than what has been 448

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observed in flank flow regimes such as the transient divide at the EDML drill site ($\Delta \lambda_H > 0.3$, Ershadi and others (2022)). Based on these comparisons, it appears that HIR in terms of its ice-fabric characteristic is not older than 4 times t_D (i.e., not older than approximately 5600 years). However, given the discrepancies between the model assumptions and observations, this time interval is not well constrained.

454 Taken together, the UWB radar profile across the saddle suggests a temporally stable divide position. 455 The data at the dome are less conclusive in that sense, because arch amplitudes are smaller and because the ice fabric is only weakly developed. One plausible scenario uniting this would be that HIR undergoes a 456 transition from a promontory towards an isle-type ice rise, which is a feature of deglaciation scenarios in this 457 particular region (Favier and Pattyn, 2015). Thinning in the saddle area would then result in comparatively 458 large arches relative to today's ice thickness in this area. The good match to the ice-core data reinforces 459 that quad-polarimetric surveys can be a reliable tool to further constrain ice-rise evolution, in particular 460 the influence of ice-anisotropy on Raymond arch evolution. For HIR, the comparatively weak ice -fabric 461 suggests a comparatively young dome. However, a single two-dimensional profile heavily simplifies the 462 dynamic complexity and modeling should account for these three-dimensional effects in the future. 463

464 6. CONCLUSION

We have investigated radar-derived properties of Hammarryggen Ice Rise (HIR): radar stratigraphy, strain rates, and ice-fabrics. HIR is a representative triple junction promontory ice-rise, making it an excellent laboratory to study ice dynamic processes, where we additionally, had access to both the ice core for c-axes measurements and the corresponding radar data.

Upward arching in the stratigraphy indicates a stable ice divide in the saddle area over, at least, 470 several thousands of years. Upward arching beneath the dome is also observed but is less clear. Vertical 471 strain rates are dominated by firn compaction near the surface, and exhibit a minimum closer to the 472 bed indicative for the Raymond effect. The derived ice-fabric properties from quad-polarimetric radar 473 fit ice-core-based values. The horizontal anisotropy is weak and thus young compared to steady-state, 474 ice-dynamically evolved ice-fabric types predicted from two-dimensional models in comparable settings. 475 This is perhaps indicative of thinning of the saddle connecting the dome to the mainland. There are 476 also signatures of the Raymond effect in the ice-fabric. However, it is unclear how the triple junction 477 geometry of Hammarryggen Ice Rise impacts both the vertical strain rates and the ice-fabric development. 478

Previous studies have indicated that the region is ice-dynamically stable and comparatively resilient to sea-level changes (Drews and others, 2015; Favier and Pattyn, 2015). Our study on Hammarryggen Ice Rise provides further evidence for this stability, although it is the first instance where we suspect the dome position may have a younger history compared to the connected saddle. This could be an important consideration when using ice rises as proxies for ice-dynamic changes in their respective catchments.

Overall, the synthesis of the different radar observations has the potential to constrain unknown parameters like the ice fabric in future ice-flow modeling, particularly if measurements cover larger areas. We suggest that these additional geophysical constraints provide another step forward towards a quantitative interpretation of Raymond arch amplitudes using observationally constrained, anisotropic, three-dimensional ice-flow models of triple junctions, flow regimes common to many ice rises around Antarctica. To better understand the ice fabric and the dynamics of a triple junction ice rise, it is advised that future pRES measurement campaigns have profiles perpendicular to each ridge.

492 7. CODE AND DATA AVAILABILITY.

493 The source code used in this study for pRES fabric analysis, strain rate analysis, and SIA 494 is available at https://github.com/RezaErshadi/HammarryggenIceRiseSourceCode_FabricInversion_ 495 Strainrates_SIA. The pRES and ice core data can be accessed at https://zenodo.org/record/8095508, 496 and the UWB data is available in Franke and others (2020), and Koch and others (2023b).

497 8. AUTHOR CONTRIBUTIONS.

M. Reza Ershadi led the code development and writing of the manuscript. Frank Pattyn and Sainan Sun collected the pRES data at HIR. Veronica Tsibulskaya, Jean-Louis Tison, Sarah Wauthy led the ice core analysis. M. Reza Ershadi, Reinhard Drews and Carlos Martin designed the study outline. M. Reza Ershadi analyzed the pRES data. Reinhard Drews, Inka Koch and Olaf Eisen led the UWB data analysis and interpretation. A. Clara J. Henry designed the SIA model. Falk M. Oraschewski inferred the vertical strain rate. Paul Bons and Jean-Louis Tison led the interpretation of the fabric type. All authors contributed to the writing of the final paper.

505 9. COMPETING INTERESTS.

506 Co-author Frank Pattyn is an associate chief editor in JOG.

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524 References

- 525 Alfred-Wegener-Institut Helmholtz-Zentrum für Polar- und Meeresforschung (2016) Polar aircraft Polar5
- and Polar6 operated by the Alfred Wegener Institute. Journal of Large-Scale Research Facilities, 2, A87–
 A87 (doi: 10.17815/jlsrf-2-153)
- Alley RB (1992) Flow-Law Hypotheses for Ice-Sheet Modeling. Journal of Glaciology, 38(129), 245–256
 (doi: 10.3189/S0022143000003658)
- 530 Bentley MJ, Ó Cofaigh C, Anderson JB, Conway H, Davies B, Graham AGC, Hillenbrand CD, Hodgson DA,
- Jamieson SSR, Larter RD, Mackintosh A, Smith JA, Verleyen E, Ackert RP, Bart PJ, Berg S, Brunstein

533

535

D, Canals M, Colhoun EA, Crosta X, Dickens WA, Domack E, Dowdeswell JA, Dunbar R, Ehrmann 532

W, Evans J, Favier V, Fink D, Fogwill CJ, Glasser NF, Gohl K, Golledge NR, Goodwin I, Gore DB,

- Greenwood SL, Hall BL, Hall K, Hedding DW, Hein AS, Hocking EP, Jakobsson M, Johnson JS, Jomelli 534
- V, Jones RS, Klages JP, Kristoffersen Y, Kuhn G, Leventer A, Licht K, Lilly K, Lindow J, Livingstone SJ,
- Massé G, McGlone MS, McKay RM, Melles M, Miura H, Mulvaney R, Nel W, Nitsche FO, O'Brien PE, 536
- 537 Post AL, Roberts SJ, Saunders KM, Selkirk PM, Simms AR, Spiegel C, Stolldorf TD, Sugden DE, van
- 538 der Putten N, van Ommen T, Verfaillie D, Vyverman W, Wagner B, White DA, Witus AE and Zwartz
- D (2014) A Community-Based Geological Reconstruction of Antarctic Ice Sheet Deglaciation since the 539
- Last Glacial Maximum. Quaternary Science Reviews, 100, 1–9 (doi: 10.1016/j.quascirev.2014.06.025) 540
- Bons PD, Kleiner T, Llorens MG, Prior DJ, Sachau T, Weikusat I and Jansen D (2018) Greenland Ice Sheet: 541
- Higher Nonlinearity of Ice Flow Significantly Reduces Estimated Basal Motion. Geophysical Research 542 Letters, 45(13), 6542–6548 (doi: 10.1029/2018GL078356) 543
- Brennan PV, Lok LB, Nicholls K and Corr H (2014) Phase-sensitive FMCW radar system for high-544 precision Antarctic ice shelf profile monitoring. IET Radar, Sonar & Navigation, 8(7), 776–786 (doi: 545 10.1049/iet-rsn.2013.0053) 546
- Budd WF and Jacka TH (1989) A Review of Ice Rheology for Ice Sheet Modelling. Cold Regions Science 547 and Technology, 16(2), 107–144 (doi: 10.1016/0165-232X(89)90014-1) 548
- Cavitte MGP, Goosse H, Wauthy S, Kausch T, Tison JL, Liefferinge BV, Pattyn F, Lenaerts JTM 549 and Claeys P (2022) From Ice Core to Ground-Penetrating Radar: Representativeness of SMB at 550 three ice rises along the Princess Ragnhild Coast, East Antarctica. Journal of Glaciology, 1–13 (doi: 551 10.1017/jog.2022.39) 552
- Conway H and Wilbour C (1999) Evolution of snow slope stability during storms1. Cold Regions Science 553 and Technology, **30**(1), 67–77 (doi: 10.1016/S0165-232X(99)00009-9) 554
- CReSIS (2021) Cresis Toolbox [computer software] (doi: 10.5281/zenodo.5683959), retrieved from GitHub 555 Dall J (2010) Ice Sheet Anisotropy Measured with Polarimetric Ice Sounding Radar. In 2010 IEEE 556 International Geoscience and Remote Sensing Symposium, 2507–2510 (doi: 10.1109/IGARSS.2010. 557 5653528) 558
- Davies BJ, Hambrey MJ, Smellie JL, Carrivick JL and Glasser NF (2012) Antarctic Peninsula Ice Sheet 559 evolution during the Cenozoic Era. Quaternary Science Reviews, **31**, 30–66 (doi: 10.1016/j.quascirev. 560 2011.10.012) 561

- 24
- 562 Drews R, Martín C, Steinhage D and Eisen O (2013) Characterizing the Glaciological Conditions at
- Halvfarryggen ice dome, Dronning Maud Land, Antarctica. Journal of Glaciology, 59(213), 9–20 (doi:
 10.3189/2013JoG12J134)
- Drews R, Matsuoka K, Martín C, Callens D, Bergeot N and Pattyn F (2015) Evolution of Derwael Ice Rise
 in Dronning Maud Land, Antarctica, over the last millennia. Journal of Geophysical Research: Earth
 Surface, 120(3), 564–579 (doi: 10.1002/2014JF003246)
- Durand G, Gillet-Chaulet F, Svensson A, Gagliardini O, Kipfstuhl S, Meyssonnier J, Parrenin F, Duval
 P and Dahl-Jensen D (2007) Change in Ice Rheology during Climate Variations implications for
 ice flow modelling and dating of the EPICA Dome C core. *Climate of the Past*, 3(1), 155–167 (doi:
 10.5194/cp-3-155-2007)
- Ershadi MR, Drews R, Martín C, Eisen O, Ritz C, Corr H, Christmann J, Zeising O, Humbert A and
 Mulvaney R (2022) Polarimetric Radar Reveals the Spatial Distribution of Ice Fabric at Domes and
 Divides in East Antarctica. *The Cryosphere*, 16(5), 1719–1739 (doi: 10.5194/tc-16-1719-2022)
- Ershadi MR, Drews R, Hawkins JD, Elliott J, Lines AP, Koch I and Eisen O (2024) Autonomous Rover
 Enables Radar Profiling of Ice-Fabric Properties in Antarctica. *IEEE Transactions on Geoscience and Remote Sensing*, 62, 1–9 (doi: 10.1109/TGRS.2024.3394594)
- Favier L and Pattyn F (2015) Antarctic Ice Rise Formation, Evolution, and Stability. *Geophysical Research Letters*, 42(11), 4456–4463 (doi: 10.1002/2015GL064195)
- Favier L, Gagliardini O, Durand G and Zwinger T (2012) A Three-Dimensional Full Stokes model of the
 grounding line dynamics: Effect of a pinning point beneath the ice shelf. *The Cryosphere*, 6(1), 101–112
 (doi: 10.5194/tc-6-101-2012)
- Favier L, Durand G, Cornford SL, Gudmundsson GH, Gagliardini O, Gillet-Chaulet F, Zwinger T, Payne
 AJ and Le Brocq AM (2014) Retreat of Pine Island Glacier controlled by marine ice-sheet instability.
- 585 Nature Climate Change, 4(2), 117–121 (doi: 10.1038/nclimate2094)
- 586 Franke S, Jansen D, Drews R and Eisen O (2020) Ice thickness from the coast of Dronning Maud Land
- 587 (Antarctica), recorded 2018/19 with the AWI UWB radar system (doi: 10.1594/PANGAEA.911868),
- alfred Wegener Institute, Helmholtz Centre for Polar and Marine Research, Bremerhaven
- 589 Franke S, Eisermann H, Jokat W, Eagles G, Asseng J, Miller H, Steinhage D, Helm V, Eisen O and Jansen
- 590 D (2021) Preserved landscapes underneath the Antarctic Ice Sheet reveal the geomorphological history of
- Jutulstraumen Basin. Earth Surface Processes and Landforms, 46(13), 2728–2745 (doi: 10.1002/esp.5203)

- Franke S, Jansen D, Binder T, Paden JD, Dörr N, Gerber TA, Miller H, Dahl-Jensen D, Helm V, Steinhage
 D, Weikusat I, Wilhelms F and Eisen O (2022) Airborne ultra-wideband radar sounding over the shear
 margins and along flow lines at the onset region of the Northeast Greenland Ice Stream. *Earth System Science Data*, 14(2), 763-779 (doi: 10.5194/essd-14-763-2022)
- Fromm T, Oberdieck C, Heitland T and Köhler P (2019) Expeditions to Antarctica: ANT-Land 2018/19
 Neumayer Station III, Kohnen Station, Flight Operations and Field Campaigns (doi: 10.2312/BzPM\
 <u>0733</u>2019)
- Fujita S, Maeno H and Matsuoka K (2006) Radio-Wave Depolarization and Scattering within Ice Sheets:
 A Matrix-Based Model to Link Radar and Ice-Core Measurements and Its Application. Journal of *Glaciology*, 52(178), 407–424 (doi: 10.3189/172756506781828548)
- Gillet-Chaulet F, Hindmarsh RCA, Corr HFJ, King EC and Jenkins A (2011) In-situquantification of ice
 rheology and direct measurement of the raymond effect at summit, greenland using a phase-sensitive
 radar. *Geophysical Research Letters*, 38(24), L24503 (doi: 10.1029/2011GL049843)
- Goel V, Brown J and Matsuoka K (2017) Glaciological Settings and Recent Mass Balance of Blåskimen
 Island in Dronning Maud Land, Antarctica. *The Cryosphere*, **11**(6), 2883–2896 (doi: 10.5194/
 tc-11-2883-2017)
- Goel V, Martín C and Matsuoka K (2018) Ice-Rise Stratigraphy Reveals Changes in Surface Mass
 Balance over the Last Millennia in Dronning Maud Land. Journal of Glaciology, 64(248), 932–942 (doi:
 10.1017/jog.2018.81)
- Goel V, Matsuoka K, Berger CD, Lee I, Dall J and Forsberg R (2020) Characteristics of Ice Rises and
 Ice Rumples in Dronning Maud Land and Enderby Land, Antarctica. *Journal of Glaciology*, 66(260),
- 613 1064–1078 (doi: 10.1017/jog.2020.77)
- Greve R and Blatter H (2009) Dynamics of Ice Sheets and Glaciers. Advances in Geophysical and
 Environmental Mechanics and Mathematics, Springer, ISBN 978-3-642-03414-5 978-3-642-03415-2 (doi:
 10.1007/978-3-642-03415-2)
- Hale R, Miller H, Gogineni S, Yan JB, Rodriguez-Morales F, Leuschen C, Paden J, Li J, Binder T,
 Steinhage D, Gehrmann M and Braaten D (2016) Multi-channel ultra-wideband radar sounder and
- 619 imager. In 2016 IEEE International Geoscience and Remote Sensing Symposium (IGARSS), 2112–2115
- 620 (doi: 10.1109/IGARSS.2016.7729545)

621 Hamilton GS and Whillans IM (2000) Point Measurements of Mass Balance of the Greenland Ice Sheet

- using precision vertical Global Positioning System (GPS) surveys. Journal of Geophysical Research: Solid
 Earth, 105(B7), 16295–16301 (doi: 10.1029/2000JB900102)
- Hargreaves ND (1977) The polarization of radio signals in the radio echo sounding of ice sheets. Journal of *Physics D: Applied Physics*, **10**(9), 1285–1304 (doi: 10.1088/0022-3727/10/9/012)
- 626 Hargreaves ND (1978) The Radio-Frequency Birefringence of Polar Ice. Journal of Glaciology, 21(85), 301–
- 627 313 (doi: 10.3189/S0022143000033499)
- 628 Henry ACJ, Drews R, Schannwell C and Višnjević V (2022) Hysteretic Evolution of Ice Rises and Ice
- Rumples in Response to Variations in Sea Level. *EGUsphere*, 1–25 (doi: 10.5194/egusphere-2022-128)
- 630 Hindmarsh RCA, King EC, Mulvaney R, Corr HFJ, Hiess G and Gillet-Chaulet F (2011) Flow at Ice-Divide
- 631 Triple Junctions: 2. Three-dimensional views of isochrone architecture from ice-penetrating radar surveys.
- 632 Journal of Geophysical Research: Earth Surface, **116**(F2), F02024 (doi: 10.1029/2009JF001622)
- Holschuh N, Christianson K and Anandakrishnan S (2014) Power loss in dipping internal reflectors, imaged
 using ice-penetrating radar. Annals of Glaciology, 55(67), 49–56 (doi: 10.3189/2014AoG67A005)
- 635 Howat I, Porter C, Noh MJ, Husby E, Khuvis S, Danish E, Tomko K, Gardiner J, Negrete A, Yadav B,
- 636 Klassen J, Kelleher C, Cloutier M, Bakker J, Enos J, Arnold G, Bauer G and Morin P (2022) The
- 637 Reference Elevation Model of Antarctica Strips, Version 4.1 (doi: 10.7910/DVN/X7NDNY)
- 638 Hutter K (1983) Theoretical Glaciology. Springer Netherlands (doi: 10.1007/978-94-015-1167-4)
- 639 Jordan TM, Schroeder DM, Castelletti D, Li J and Dall J (2019) A Polarimetric Coherence Method to
- 640 Determine Ice Crystal Orientation Fabric From Radar Sounding: Application to the NEEM Ice Core
- Region. IEEE Transactions on Geoscience and Remote Sensing, 57(11), 8641–8657 (doi: 10.1109/TGRS.
 2019.2921980)
- Jordan TM, Schroeder DM, Elsworth CW and Siegfried MR (2020) Estimation of Ice Fabric within Whillans
 Ice Stream using polarimetric phase-sensitive radar sounding. Annals of Glaciology, 61(81), 74–83 (doi:
 10.1017/aog.2020.6)
- Kingslake J, Hindmarsh RCA, Aðalgeirsdóttir G, Conway H, Corr HFJ, Gillet-Chaulet F, Martín C, King
 EC, Mulvaney R and Pritchard HD (2014) Full-depth englacial vertical ice sheet velocities measured
 using phase-sensitive radar. Journal of Geophysical Research: Earth Surface, 119(12), 2604–2618 (doi:
 10.1002/2014JF003275)

- Koch I, Drews R, Franke S, Jansen D, Oraschewski FM, Muhle LS, Višnjević V, Matsuoka K, Pattyn F
 and Eisen O (2023a) Radar internal reflection horizons from multisystem data reflect ice dynamic and
 surface accumulation history along the Princess Ragnhild Coast, Dronning Maud Land, East Antarctica. *Journal of Glaciology*, 1–19 (doi: 10.1017/jog.2023.93)
- 654 Koch I, Drews R, Muhle LS, Franke S, Jansen D, Oraschewski F, Spiegel H, Višnjević V, Matsuoka K, Pattyn
- F and Eisen O (2023b) Internal reflection horizons of ice shelves and ice rises in eastern Dronning Maud
- Land (East Antarctica) from multisystem radio-echo sounding data (doi: 10.1594/PANGAEA.950383)
- Langway CC (1958) Ice Fabrics and the Universal Stage. Technical Report SIPRE report ; 62, U.S. Army
 Snow, Ice, and Permafrost Research Establishment, Engineer Research and Development Center (U.S.),
- approved for public release; distribution is unlimited. http://hdl.handle.net/11681/6005
- Lenaerts JTM, Brown J, Broeke MRVD, Matsuoka K, Drews R, Callens D, Philippe M, Gorodetskaya
 IV, Meijgaard EV, Reijmer CH, Pattyn F and Lipzig NPMV (2014) High variability of climate and
 surface mass balance induced by Antarctic ice rises. *Journal of Glaciology*, 60(224), 1101–1110 (doi:
 10.3189/2014JoG14J040)
- Llorens MG, Griera A, Bons PD, Weikusat I, Prior DJ, Gomez-Rivas E, de Riese T, Jimenez-Munt
 I, García-Castellanos D and Lebensohn RA (2022) Can changes in deformation regimes be inferred
 from crystallographic preferred orientations in polar ice? *The Cryosphere*, 16(5), 2009–2024 (doi:
 10.5194/tc-16-2009-2022)
- Martín C and Gudmundsson GH (2012) Effects of Nonlinear Rheology, Temperature and Anisotropy
 on the Relationship between Age and Depth at Ice Divides. *The Cryosphere*, 6(5), 1221–1229 (doi:
 10.5194/tc-6-1221-2012)
- Martín C, Hindmarsh RCA and Navarro FJ (2006) Dating ice flow change near the flow divide at
 Roosevelt Island, Antarctica, by using a thermomechanical model to predict radar stratigraphy. *Journal*of Geophysical Research: Earth Surface, 111(F1), F01011 (doi: 10.1029/2005JF000326)
- Martín C, Gudmundsson GH, Pritchard HD and Gagliardini O (2009a) On the effects of anisotropic rheology
 on ice flow, internal structure, and the age-depth relationship at ice divides. *Journal of Geophysical Research: Earth Surface*, 114(F4), F04001 (doi: 10.1029/2008JF001204)
- 677 Martín C, Hindmarsh RCA and Navarro FJ (2009b) On the effects of divide migration, along-ridge flow, and
- basal sliding on isochrones near an ice divide. Journal of Geophysical Research: Earth Surface, 114(F2),
- 679 F02006 (doi: 10.1029/2008JF001025)

- Matsuoka K, Hindmarsh RC, Moholdt G, Bentley MJ, Pritchard HD, Brown J, Conway H, Drews R,
 Durand G, Goldberg D, Hattermann T, Kingslake J, Lenaerts JT, Martín C, Mulvaney R, Nicholls
 KW, Pattyn F, Ross N, Scambos T and Whitehouse PL (2015) Antarctic Ice Rises and Rumples: Their
 properties and significance for ice-sheet dynamics and evolution. *Earth-Science Reviews*, 150, 724–745
- 684 (doi: 10.1016/j.earscirev.2015.09.004)
- Matsuoka T, Fujita S, Morishima S and Mae S (1997) Precise measurement of dielectric anisotropy in ice
 Ih at 39 GHz. Journal of Applied Physics, 81(5), 2344–2348 (doi: 10.1063/1.364238)
- 687 Morlighem M (2022) MEaSUREs BedMachine Antarctica, Version 3 (doi: 10.5067/FPSU0V1MWUB6)
- 688 Morlighem M, Rignot E, Binder T, Blankenship D, Drews R, Eagles G, Eisen O, Ferraccioli F, Forsberg
- R, Fretwell P, Goel V, Greenbaum JS, Gudmundsson H, Guo J, Helm V, Hofstede C, Howat I, Humbert
- A, Jokat W, Karlsson NB, Lee WS, Matsuoka K, Millan R, Mouginot J, Paden J, Pattyn F, Roberts J,
- Rosier S, Ruppel A, Seroussi H, Smith EC, Steinhage D, Sun B, van den Broeke MR, van Ommen TD,
 van Wessem M and Young DA (2020) Deep Glacial Troughs and Stabilizing Ridges Unveiled beneath the
- Margins of the Antarctic ice sheet. Nature Geoscience, 13(2), 132–137 (doi: 10.1038/s41561-019-0510-8)
 Nereson NA and Waddington ED (2002) Isochrones and Isotherms beneath Migrating Ice Divides. Journal
 of Glaciology, 48(160), 95–108 (doi: 10.3189/172756502781831647)
- Nereson NA, Hindmarsh RCA and Raymond CF (1998) Sensitivity of the Divide Position at Siple
 Dome, West Antarctica, to boundary forcing. Annals of Glaciology, 27, 207–214 (doi: 10.3189/
 1998AoG27-1-207-214)
- Nicholls KW, Corr HF, Stewart CL, Lok LB, Brennan PV and Vaughan DG (2015) A ground-based radar
 for measuring vertical strain rates and time-varying basal melt rates in ice sheets and shelves. *Journal of Glaciology*, 61(230), 1079–1087 (doi: 10.3189/2015JoG15J073)
- Passchier CW (1997) The Fabric Attractor. Journal of Structural Geology, 19(1), 113–127 (doi: 10.1016/
 S0191-8141(96)00077-6)
- Pattyn F, Wauthy S, Sun S, Tison JL and Tsibulskaya V (2023) Polarimetric Radar Data and Ice Core
 Data Collected at Hammarryggen Ice Rise, Antarctica (doi: 10.5281/zenodo.8095508)
- 706 Petit RJ, Aguinagalde I, de Beaulieu JL, Bittkau C, Brewer S, Cheddadi R, Ennos R, Fineschi S, Grivet
- 707 D, Lascoux M, Mohanty A, Müller-Starck G, Demesure-Musch B, Palmé A, Martín JP, Rendell S and
- Vendramin GG (2003) Glacial Refugia: Hotspots but Not Melting Pots of Genetic Diversity. Science
- 709 (New York, N.Y.), **300**(5625), 1563–1565 (doi: 10.1126/science.1083264)

- Philippe M, Tison JL, Fjøsne K, Hubbard B, Kjær HA, Lenaerts JTM, Drews R, Sheldon SG, De Bondt 710
- K, Claevs P and Pattyn F (2016) Ice Core Evidence for a 20th Century Increase in Surface Mass 711
- Balance in Coastal Dronning Maud Land, East Antarctica. The Cryosphere, 10(5), 2501–2516 (doi: 712 10.5194/tc-10-2501-2016) 713
- Rathmann NM, Lilien DA, Grinsted A, Gerber TA, Young TJ and Dahl-Jensen D (2022) On the Limitations 714
- 715 of Using Polarimetric Radar Sounding to Infer the Crystal Orientation Fabric of Ice Masses. Geophysical Research Letters, **49**(1), e2021GL096244 (doi: 10.1029/2021GL096244)
- Raymond CF (1983) Deformation in the Vicinity of Ice Divides. Journal of Glaciology, 29(103), 357–373 717 (doi: 10.3189/S0022143000030288)
- Rignot E, Mouginot J and Scheuchl B (2017) MEaSURES InSAR-Based Antarctica Ice Velocity Map, 719 Version 2 (doi: 10.5067/D7GK8F5J8M8R) 720
- Rodriguez-Morales F, Gogineni S, Leuschen CJ, Paden JD, Li J, Lewis CC, Panzer B, Gomez-721 Garcia Alvestegui D, Patel A, Byers, Crowe, Player, Hale, Arnold, Smith, Gifford, Braaten and Panton 722 (2014) Advanced Multifrequency Radar Instrumentation for Polar Research. IEEE Transactions on 723
- Geoscience and Remote Sensing, 52(5), 2824–2842 (doi: 10.1109/TGRS.2013.2266415) 724
- Schannwell C, Drews R, Ehlers TA, Eisen O, Mayer C and Gillet-Chaulet F (2019) Kinematic Response of 725 Ice-Rise Divides to Changes in Ocean and Atmosphere Forcing. The Cryosphere, 13(10), 2673–2691 (doi: 726 10.5194/tc-13-2673-2019) 727
- Schannwell C, Drews R, Ehlers TA, Eisen O, Mayer C, Malinen M, Smith EC and Eisermann H (2020) 728 Quantifying the Effect of Ocean Bed Properties on Ice Sheet Geometry over 40 000 Years with a Full-729 Stokes model. The Cryosphere, 14(11), 3917–3934 (doi: 10.5194/tc-14-3917-2020) 730
- Sun S, Hattermann T, Pattyn F, Nicholls KW, Drews R and Berger S (2019) Topographic Shelf Waves 731
- Control Seasonal Melting Near Antarctic Ice Shelf Grounding Lines. Geophysical Research Letters, 46(16), 732 9824–9832 (doi: 10.1029/2019GL083881) 733
- Wauthy S, Tison JL, Inoue M, El Amri S, Sun S, Fripiat F, Claeys P and Pattyn F (2024) Spatial and 734
- temporal variability of environmental proxies from the top 120 m of two ice cores in dronning maud land 735
- (east antarctica). Earth System Science Data, 16(1), 35–58 (doi: 10.5194/essd-16-35-2024) 736
- Wilson CJL, Russell-Head DS and Sim HM (2003) The Application of an Automated Fabric Analyzer 737
- System to the Textural Evolution of Folded Ice Layers in Shear Zones. Annals of Glaciology, 37, 7–17 738
- (doi: 10.3189/172756403781815401) 739

716

718

- 740 Woodcock NH (1977) Specification of Fabric Shapes Using an Eigenvalue Method. Geological Society of
- 741 America Bulletin, 88(9), 1231 (doi: 10.1130/0016-7606(1977)88<1231:SOFSUA>2.0.CO;2)
- 742 Young TJ, Martín C, Christoffersen P, Schroeder DM, Tulaczyk SM and Dawson EJ (2021) Rapid and
- accurate polarimetric radar measurements of ice crystal fabric orientation at the western antarctic ice
- sheet (wais) divide ice core site. The Cryosphere, 15(8), 4117-4133 (doi: 10.5194/tc-15-4117-2021)
- 745 Zeising O, Gerber TA, Eisen O, Ershadi MR, Stoll N, Weikusat I and Humbert A (2023) Improved
- 746 Estimation of the Bulk Ice Crystal Fabric Asymmetry from Polarimetric Phase Co-Registration. The
- 747 Cryosphere, **17**(3), 1097–1105 (doi: 10.5194/tc-17-1097-2023)

748 Appendix A. LIMITATIONS IN DEPTH OF INVESTIGATION

In figure A1, we present the signal power (blue line) and coherence magnitude (red line) at the p0 radar site (located at the centre of the profile). As detailed in Section 3.1, if the coherence magnitude falls below 0.4 (Fig. A1 - red zone), the signal is considered unreliable for further phase analysis. As depicted in the figure, the coherence magnitude falls below 0.4 at approximately 400 m depth. As a result, for all pRES data analyzed in this study, only the top 400 m are used.



Figure A1: (a) Radar backscattered power (blue line) reveals the ice thickness. (b) The magnitude of complex polarimetric coherence between HH and VV signal (red line). The red zone is the area below 0.4 coherence magnitude.

755 Appendix B. 2D INTERPOLATED FABRIC SPATIAL CHANGE

A 2D interpolated spatial distribution of fabric properties inferred from pRES data is provided in figure B1. The values depicted in figure. B1a and B1b represent $\Delta\lambda_H$ and λ_3 , respectively, directly estimated from the pRES data. On the other hand, figure B1c and B1d illustrate the deviation between the estimated ice fabric orientation \vec{v}_2 and the surface flow direction from SIA and between \vec{v}_2 and the maximum strain direction from SIA, respectively.



Figure B1: Showing the two dimensional interpolation of (a) horizontal ice fabric anisotropy. (b) Magnitude of the strongest eigenvalue (*lambda*₃). (c) deviation of \vec{v}_2 from surface flow direction. (d) deviation of \vec{v}_2 from maximum strain rate direction. Not that both X and Y axes are normalized by the mean ice thickness (H \simeq 550 m).

761 Appendix C. WOODCOCK PLOT (PRES AND ICE CORE)

Woodcock (1977) introduced the parameter $K = \frac{\ln(\lambda_3/\lambda_2)}{\ln(\lambda_2/\lambda_1)}$ as a logarithmic ratio between the Eigenvalues, dividing the ice fabric type into the cluster zone (K > 1) and the girdle zone (K < 1). The extreme cases are the uniaxial girdle (K close to 0) and the uniaxial cluster (K close to infinity), with K = 1 representing the transition zone. Additionally, Woodcock introduced the parameter $C = \ln(\lambda_3/\lambda_1)$ as a measure of the preferred orientation strength. Higher C values indicate a greater concentration of the c-axis and a lower noise level. By using Woodcock's method, the ice fabric type obtained from estimated and measured Eigenvalues can be compared.

Here we regenerated the figure 1 from Woodcock (1977) and added some extra information to it. Hand-770 drawn Schmidt diagrams illustrate the shape of the ice fabric type in each zone, where the top left and 771 bottom right show the uniaxial cluster and the uniaxial girdle, respectively. The isotropic ice fabric is 772 situated at the origin of the figure. Not that the thin sections in Schmidt diagrams from the ice core 773 analysis in Fig 4c are vertical while the Schmidt diagrams shown in Fig C1 are oblique. The estimated and 774 measured ice fabric types are depicted as green squares and black circles, respectively, within the 50 to 260 775 m range. Both the estimated and measured ice fabric types suggest that the fabric is in the weak cluster 776 zone, although the estimated fabric is slightly weaker compared to the measured fabric. 777

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Figure C1: Regenerated Woodcock (1977), categorizing the ice fabric type according to Woodcock's parameters. The background color shows the change of $\Delta \lambda_H$, green dashed contours show the $\Delta \lambda_V$, blue dashed contours represent the K values, and red contours are the C values. The Schmidt diagrams are copied directly from Woodcock (1977). The green squares and black circles are estimated from radar data and measured from the ice core, respectively, between 50 to 260 m depth.

778 Appendix D. SIA RESULTS

- The magnitude and orientation of surface velocity along with the magnitude and orientation of the maximum
- 780 horizontal strain estimated from SIA as explained in section 3.5 are shown all over HIR in figure D1



Figure D1: Estimated from SIA, (a) magnitude and direction of surface velocity. (b) magnitude and direction of maximum horizontal strain rate.